

Package ‘FDOTT’

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Description Perform optimal transport based tests in factorial designs as introduced in Groppe et al. (2025) <[doi:10.48550/arXiv.2509.13970](https://doi.org/10.48550/arXiv.2509.13970)> via the FDOTT() function. These tests are inspired by ANOVA and its nonparametric counterparts. They allow for testing linear relationships in factorial designs between finitely supported probability measures on a metric space. Such relationships include equality of all measures (no treatment effect), interaction effects between a number of factors, as well as main and simple factor effects.

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cost_matrix_lp	<i>Cost Matrix of ℓ^p-Form.</i>
----------------	---

Description

Compute cost matrices of ℓ^p -form.

Usage

```
cost_matrix_lp(x, y = NULL, p = 2, q = 1)
```

Arguments

x	matrix of size $n \times d$ containing vectors $x_1, \dots, x_n \in \mathbb{R}^d$ (row-wise).
y	matrix of size $m \times d$ containing vectors $y_1, \dots, y_m \in \mathbb{R}^d$ (row-wise); $y = \text{NULL}$ means that $y_i = x_i$.
p	number $p \in (0, \infty]$.
q	number $q \in (0, \infty)$.

Value

A $n \times m$ matrix with entry at i, j being equal to

$$\|x_i - y_j\|_p^q = \left[\sum_{k=1}^d |x_{i,k} - y_{j,k}|^p \right]^{q/p}$$

For $p = \text{Inf}$, this is to be understood as the maximum norm to the power of q .

Examples

```
n <- 3
m <- 4
d <- 5
x <- runif(n * d) |> matrix(n, d)
y <- runif(m * d) |> matrix(m, d)
costm <- cost_matrix_lp(x, y)
print(costm)
```

FDOTT	<i>Test linear relationships between probability vectors in factorial designs</i>
-------	---

Description

Perform FDOTT, an optimal transport (OT) based test in factorial designs, to test linear relationships between probability vectors, based on samples from them.

Usage

```
FDOTT(
  samples,
  costm,
  H0 = "*",
  fac.names = NULL,
  method = c("plug-in", "bootstrap-deriv", "bootstrap-m", "permutation"),
  num.sim = 1000,
  null.mu = NULL,
  m.p = 0.5,
  is.metric = is_metric_cost_mat(costm, tol.ti = Inf),
  verbose = FALSE
)

FDOTT2(
  formula,
  costm,
  data = NULL,
  method = c("plug-in", "bootstrap-deriv", "bootstrap-m", "permutation"),
  num.sim = 1000,
  null.mu = NULL,
  m.p = 0.5,
  is.metric = is_metric_cost_mat(costm, tol.ti = Inf),
  verbose = FALSE
)
```

Arguments

<code>samples</code>	nested list of depth D (representing a D -way layout) containing count vectors. A count vector is a vector of length N that contains the number of times a sample was observed at the respective points. Can also be given as a matrix (row-wise), which is viewed as a one-way layout.
<code>costm</code>	semi-metric cost matrix $c \in \mathbb{R}^{N \times N}$ between the N values the observations can take.
<code>H0</code>	null hypothesis, see details.

fac.names	names of the D factors. Used for printing. Default NULL corresponds to "F1" for factor 1, and so on.
method	the method to use to simulate from the null distribution, see details.
num.sim	number of samples to draw from the limiting null distribution.
null.mu	probability vectors μ underlying the null distribution used only for method = "plug-in". Must be a nested list or a matrix (row-wise, in lexicographical order of the factors).
m.p	exponent $p \in (0, 1)$ used only for method = "bootstrap-m".
is.metric	value indicating whether c is a metric cost matrix, see is_metric_cost_mat .
verbose	logical value indicating whether additional information should be printed.
formula	an object of class "formula" specifying the samples, layout and effects to test, see details.
data	object (e.g. a data.frame) containing the variables for formula.

Details

Denote with μ the matrix (row-wise) of the probability vectors (in lexicographical order of the factor combinations) that underlie samples or are specified via formula. FDOTT deals with null hypotheses of the form

$$H_0^L : L\mu = 0,$$

where L is a suitable matrix with row sums all equal to 0. The FDOTT statistic is defined as

$$T^L(\hat{\mu}_n) := \frac{\sqrt{\rho_n}}{s} \sum_{m=1}^M \text{OT}_c^\pm([L\hat{\mu}_n]_m, 0),$$

where ρ_n and s are scaling factors, $[L\mu]_m$ is the m -th row-vector of $L\mu$ and $\text{OT}_c^\pm$ the extended OT functional, see [ot_cost_sgn](#). The test is based on the asymptotic distribution of $T^L(\hat{\mu}_n)$ under the null, for more details see Groppe et al. (2025).

The form of H_0^L allows for testing hypotheses like interaction effects in classical ANOVA, obtained by formally substituting means by measures. The null hypothesis can be either specified via H_0 (in FDOTT) or in formula (in FDOTT2). The following values are allowed for H_0 :

- $H_0 = "*"$ (the default). Test all interaction (including main effects) of the factors. A specific interaction or main effect can be tested by including the corresponding indices of the factors with ":" in a list, e.g., $H_0 = \text{list}(":", c(1, 3))$ corresponds to the interaction effect between factor 1 and 3. Note that in a one-way layout, $H_0 = "*"$ reduces to $H_0 = "="$.
- $H_0 = "|"$. Test all simple factor effects (within all other remaining factors). A specific simple factor effect can be tested by including the corresponding indices of the factors in a list, e.g., $H_0 = \text{list}("|", c(1, 3))$ corresponds to the simple factor effect of factor 1 and 3 within the other remaining factors. Optionally, the within-factors can be specified via indices as the third argument in the list.
- $H_0 = "="$. Test for treatment effect, i.e., whether all underlying probability vectors are the same. Note that each pairwise comparison can be tested simultaneously via [FDOTT_HSD](#).
- $H_0 = L$. Test H_0^L for the directly supplied L matrix. The name of the tested effect (useful for printing) and the scaling s (by default $\text{nrow}(L)$) can be supplied by setting the "effect" and "scaling" attribute of L , respectively.

- `H0 = list(...)`. Test a combined null hypothesis. Each element of the list represents a null hypothesis and can be given by one of the options above. This is useful in combination with `FDOTT_HSD`, which allows to test all the given null hypotheses simultaneously.

Alternatively, the factorial design and the effects to test can be specified via formula (and data). It must have the form `samples ~ effects | layout`:

- `samples` must be a single variable that specifies the observed sample values. Must be a factor with N levels.
- `effects` gives the (simple) interaction effects to test. The notation is as in in linear models (see [lm](#)), e.g., `A * B` expands to `A + B + A:B` and means that the main effects of `A` and `B` as well as their interaction effect `A:B` should be tested. Similarly, simple factor effects can be specified as `simple(effs, within)` where `within` is optional and defaults to all factors that are not in `effs`. Lastly, adding `0` (i.e., removing the intercept) is interpreted as testing for a treatment effect (one-way layout).
- `layout` (and the preceding `|`) is optional and gives the variables of the factorial design. All variables must be factors. `layout` is only needed if the factorial layout has more factors that are not already specified in `effects`. For example, a two-way layout can be reduced to the one-way layout by taking `formula = samples ~ 0 | A + B`.

To simulate from the limiting null distribution, there are four different methods:

- "plug-in": uses the limiting distribution where μ is substituted by its empirical version (or `null.mu`, when specified).
- "bootstrap-deriv": uses the so-called derivative bootstrap.
- "bootstrap-m": uses m -out-of- n bootstrap with $m = \lfloor n^p \rfloor$.
- "permutation": uses a permutation approach, only works for `H0 = "="`.

These simulations can be done in parallel via `future::plan` and the progress can be shown with `progressr::with_progress`.

Value

A FDOTT object containing:

<code>fac.lvls</code>	vector of levels of the factors
<code>mu</code>	matrix, empirical version $\hat{\mu}_n$ of μ that is based on samples
<code>n</code>	vector of sample sizes n
<code>L</code>	matrix L for the null hypothesis H_0^L
<code>p.value</code>	the p -value
<code>statistic</code>	the value of the test statistic $T^L(\hat{\mu}_n)$
<code>null.samples</code>	samples drawn from the null distribution

References

M. Groppe, L. Niemöller, S. Hundrieser, D. Ventzke, A. Blob, S. Köster and A. Munk (2025). Optimal Transport Based Testing in Factorial Design. arXiv preprint. [doi:10.48550/arXiv.2509.13970](https://doi.org/10.48550/arXiv.2509.13970).

See Also[FDOTT_HSD](#)**Examples**

```

# enable txt progressbar
progressr::handlers("txtprogressbar")
# enable parallel computation
if (requireNamespace("future")) {
  future::plan(future::multisession)
}

# use higher number to better approximate null distribution and get more accurate p-values
num.sim <- 10

### two-way layout

K1 <- K2 <- 2
N <- 3
costm <- cost_matrix_lp(1:N)

n <- list(list(300, 360), list(280, 200))

# underlying probability vectors (two-way layout)
# no interaction effect, only factor 2 has main effect
mu <- list(
  list(c(0, 0.5, 0.5), c(0.25, 0.25, 0.5)),
  list(c(0, 0.5, 0.5), c(0.25, 0.25, 0.5))
)

# test interaction effect and main effects, equivalent to H0 <- "*"
H0 <- list(list(":", 1:2), list(":", 1), list(":", 2))

set.seed(123)
samples <- tab_sample(n, mu)

res1 <- FDOTT(samples, costm, H0 = H0, num.sim = num.sim)
print(res1)

# find out exactly which effect gets rejected via HSD
res11 <- FDOTT_HSD(res1)
print(res11)

# now with interaction effect
mu[[1]][[1]] <- c(0.1, 0.1, 0.8)

## using formula instead
# first transform samples to data.frame
set.seed(123)
samples <- tab_sample(n, mu)
df <- do.call(
  rbind,

```

```

    lapply(
      1:K1,
      \(i) lapply(1:K2, \(j) data.frame(x = rep(1:N, times = samples[[c(i, j)]]), a = i, b = j))
    ) |> unlist(FALSE)
  )
df$x <- as.factor(df$x) # sample variable
df$a <- as.factor(df$a) # first factor
df$b <- as.factor(df$b) # second factor

f <- x ~ a : b # test for interaction effect only

res2 <- FDOTT2(f, costm, data = df, num.sim = num.sim, method = "bootstrap-deriv")
print(res2)

f <- x ~ 0 | a + b # check if all mu's are the same (one-way layout)

res3 <- FDOTT2(f, costm, data = df, num.sim = num.sim)
print(res3)

# only  $\mu^{1,2} = \mu^{2,2}$ 
res31 <- FDOTT_HSD(res3)
print(res31)

f <- x ~ simple(a, b) # check simple factor effect of a within b (second argument is optional here)

res4 <- FDOTT2(f, costm, data = df, num.sim = num.sim)
print(res4)

```

FDOTT_HSD

Test multiple linear relationships between probability vectors in factorial designs

Description

Perform an optimal transport based HSD test to deal with multiple comparisons simultaneously.

Usage

```
FDOTT_HSD(test, weights = NULL, group.sizes = TRUE)
```

Arguments

test	a FDOTT object, i.e., output of FDOTT .
weights	weight vector of length K . <code>weights = NULL</code> means that no weights are used. For <code>weights = TRUE</code> the standard weighting is used.
group.sizes	integer vector summing to the number of comparisons M . Used to split the null hypothesis into sub-hypotheses of the specified sizes. The default <code>group.sizes = TRUE</code> extracts these sizes from <code>test</code> . For <code>group.sizes = NULL</code> , each equation is its own group.

Details

Let $H_0^L : L\mu = 0$ be the null hypothesis of test. In the case of rejection, it is of interest to find out exactly which row-equations are not satisfied with statistical significance. To this end, $L\mu = 0$ can be split into a number of sub-hypotheses which are tested simultaneously via an approach inspired by Tukey's HSD test, see Groppe et al. (2025) for more details.

Value

A FDOTT_HSD object containing:

p.value	the p -values
statistic	the values of the test statistics
null.samples	samples drawn from the null distribution

References

M. Groppe, L. Niemöller, S. Hundrieser, D. Ventzke, A. Blob, S. Köster and A. Munk (2025). Optimal Transport Based Testing in Factorial Design. arXiv preprint. [doi:10.48550/arXiv.2509.13970](https://doi.org/10.48550/arXiv.2509.13970).

See Also

[FDOTT](#)

Examples

```
# see FDOTT for more examples

# enable parallel computation
if (requireNamespace("future")) {
  future::plan(future::multisession)
}

K <- 3
N <- 2
costm <- cost_matrix_lp(1:N)

# use higher number to better approximate null distribution and get more accurate p-value
num.sim <- 10

# underlying probability vectors (one-way layout)
# only mu^1 and mu^3 are equal
mu <- matrix(0.5, K, N, TRUE)
mu[2, ] <- c(0.2, 0.8)

n <- c(300, 360, 200)

set.seed(123)
samples <- tab_sample(n, mu)
res <- FDOTT(samples, costm, num.sim = num.sim) |> FDOTT_HSD()
# significant differences for mu^1 = mu^2 and mu^2 = mu^3
```

```
print(res)
```

is_metric_cost_mat	<i>Check metric properties of cost matrices</i>
--------------------	---

Description

Check if a cost matrix satisfies symmetry, positive definiteness and the triangle inequality.

Usage

```
is_metric_cost_mat(x, tol.sym = 1e-08, tol.pd = 0, tol.ti = 1e-08)
```

Arguments

x	numeric square matrix.
tol.sym	tolerance used to check symmetry.
tol.pd	tolerance used to check positive definiteness.
tol.ti	tolerance used to check the triangle inequality.

Details

The following three properties of a square matrix $x \in \mathbb{R}^{N \times N}$ are checked:

- symmetry; if $x_{ij} = x_{ji}$,
- positive definiteness; if $x_{ii} = 0$ and $x_{ij} > 0$ for all $i \neq j$,
- triangle inequality; if $x_{ij} \leq x_{ik} + x_{kj}$.

If symmetry and positive definiteness are satisfied, then x is called a semi-metric cost matrix. If additionally also the triangle inequality holds, then x is a metric cost matrix.

Value

A list containing logical entries `metric`, `semi.metric`, `sym`, `pos.def` and `tri.ineq` that indicate whether the corresponding property is satisfied.

See Also

[cost_matrix_lp](#)

Examples

```

x <- cost_matrix_lp(1:5)
res <- is_metric_cost_mat(x)
res2 <- is_metric_cost_mat(x^2)
# x is a metric cost matrix
print(res$metric)
# x^2 is only a semi-metric cost matrix,
# because the triangle inequality is not satisfied
print(res2$semi.metric)
print(res2$tri.ineq)

```

ot_barycenter	<i>Compute optimal transport barycenters</i>
---------------	--

Description

Compute the optimal transport (OT) barycenter of multiple probability vectors via linear programming.

Usage

```

ot_barycenter(
  mu,
  costm,
  w = NULL,
  solver = ot_test_lp_solver(),
  constr_mat = NULL
)

```

Arguments

mu	matrix (row-wise) or list containing K probability vectors of length N .
costm	cost matrix $c \in \mathbb{R}^{N \times N}$.
w	weight vector $w \in \mathbb{R}_+^K$. The default is $w = (1/K, \dots, 1/K)$.
solver	the LP solver to use, see ot_test_lp_solver .
constr_mat	the constraint matrix for the underlying LP.

Details

The OT barycenter is defined as the minimizer of the cost functional,

$$B_c^w(\mu^1, \dots, \mu^K) := \min_{\nu} \sum_{k=1}^k w_k \text{OT}_c(\mu^k, \nu),$$

where the minimum is taken over all probability vectors ν . The OT barycenter is solved via linear programming (LP) and the underlying solver can be controlled via the parameter solver.

Value

A list containing the entries cost and barycenter.

Examples

```
K <- 3
N <- 2
costm <- cost_matrix_lp(1:N)
w <- rep(1 / K, K)

# all measures are equal
mu <- matrix(1 / N, K, N, TRUE)

# to run this, a LP solver must be available for ROI (ROI.plugin.glpk by default)
if (requireNamespace("ROI.plugin.glpk")) {
  solver <- ot_test_lp_solver("glpk")
  print(ot_barycenter(mu, costm, w = w, solver = solver))
}

# not all measures are equal
mu[2, ] <- 1:N / sum(1:N)
if (requireNamespace("ROI.plugin.glpk")) {
  solver <- ot_test_lp_solver("glpk")
  print(ot_barycenter(mu, costm, w = w, solver = solver))
}
```

ot_barycenter_test	<i>Test equality of probability vectors</i>
--------------------	---

Description

Perform optimal transport (OT) barycenter based tests for equality of probability vectors in a one-way layout.

Usage

```
ot_barycenter_test(
  samples,
  costm,
  null.mu = NULL,
  w = NULL,
  num.sim = 1000,
  solver = ot_test_lp_solver(),
  is.metric = is_metric_cost_mat(costm, tol.ti = Inf),
  verbose = FALSE
)
```

Arguments

samples	matrix (row-wise) or nested list containing K count vectors. A count vector is a vector of length N that contains the number of times a sample was observed at the respective points.
costm	semi-metric cost matrix $c \in \mathbb{R}^{N \times N}$.
null.mu	probability measures μ underlying the null distribution. Must be of the same structure as samples.
w	weight vector $w \in \mathbb{R}_+^K$.
num.sim	number of samples to draw from the limiting null distribution.
solver	the LP solver to use, see ot_test_lp_solver .
is.metric	value indicating whether c is a metric cost matrix, see is_metric_cost_mat .
verbose	logical value indicating whether additional information should be printed.

Details

Denote with $\mu^1, \dots, \mu^K$ the probability measures that underlie the samples contained in samples. To test for the one-way null hypothesis $H_0 : \mu^1 = \dots = \mu^K$, this test employs the OT barycenter statistic which is defined as $T^B(\mu) := \sqrt{\rho_n} B_c^w(\mu^1, \dots, \mu^K)$, where ρ_n is a scaling factor and B_c^w is the OT barycenter functional, see [ot_barycenter](#).

The test is based on the asymptotic distribution of T^B under the null, for more details see the reference.

These simulations can be done in parallel via [future::plan](#) and the progress can be shown with [progressr::with_progress](#).

Especially for large N and K , simulating a sufficient number of samples from the limiting null distribution might take a while. Consider using [FDOTT](#) instead.

Value

An object of class "ot_barycenter_test" containing:

mu	empirical version of μ that is based on samples
n	the sample sizes
p.value	the p -value
statistic	the value of the test statistic
null.samples	samples drawn from the null distribution

References

TODO

See Also

[FDOTT](#) with $H_0 = "="$.

Examples

```

# enable txt progressbar
progressr::handlers("txtprogressbar")
# enable parallel computation
if (requireNamespace("future")) {
  future::plan(future::multisession)
}

K <- 3
N <- 2
costm <- cost_matrix_lp(1:N)

# use higher number to better approximate null distribution and get more accurate p-value
num.sim <- 10

n <- c(300, 360, 200)

# underlying probability vectors
mu <- matrix(1 / N, K, N, TRUE)

# to run this, a LP solver must be available for ROI (ROI.plugin.glpk by default)
if (requireNamespace("ROI.plugin.glpk")) {
  solver <- ot_test_lp_solver("glpk")
  set.seed(123)
  samples <- tab_sample(n, mu)
  progressr::with_progress({
    res <- ot_barycenter_test(samples, costm, num.sim = num.sim, solver = solver)
  })
  print(res)
}

# measures are not equal anymore
mu[2, ] <- 1:N / sum(1:N)

if (requireNamespace("ROI.plugin.glpk")) {
  solver <- ot_test_lp_solver("glpk")
  set.seed(123)
  samples <- tab_sample(n, mu)
  progressr::with_progress({
    res2 <- ot_barycenter_test(samples, costm, num.sim = num.sim, solver = solver)
  })
  print(res2)
}

```

ot_cost_sgn

*Compute optimal transport costs for signed measures***Description**

Compute the optimal transport (OT) cost between signed measures that have the same total mass.

Usage

```
ot_cost_sgn(mu, nu, costm, mode = c("all", "diag"))
```

Arguments

mu	matrix (row-wise) or list containing K_1 vectors of length N .
nu	matrix (row-wise) or list containing K_2 vectors of length N or NULL.
costm	cost matrix $c \in \mathbb{R}^{N \times N}$.
mode	controls which of the pairwise OT costs are computed.

Details

The extended OT functional for vectors $\mu, \nu \in \mathbb{R}^N$ with $\sum_{i=1}^N \mu_i = \sum_{i=1}^N \nu_i$ is defined as

$$\text{OT}_c^\pm(\mu, \nu) := \text{OT}_c(\mu^+ + \nu^-, \nu^+ + \mu^-),$$

where $\mu^+ = \max(0, \mu)$ and $\mu^- = -\min(0, \mu)$ denote the positive and negative part of μ , and OT_c is the standard OT functional. To compute the standard OT, the function `transport::transport` is used. The values may be computed in parallel via `future::plan`.

Value

The OT cost between the vectors in mu and nu.

For mode = "all" the whole matrix of size $K_1 \times K_2$ is returned. If mu or nu is a vector, then this matrix is also returned as a vector. nu = NULL means that nu = mu and only the lower triangular part is actually computed and then reflected.

If mode = "diag", then only the diagonal is returned (requiring $K_1 = K_2$).

See Also

`transport::transport`

Examples

```
# enable parallel computation
if (requireNamespace("future")) {
  future::plan(future::multisession)
}

# generate random signed measures with total mass 0 (row-wise)
rsum0 <- \(K, N) {
  x <- runif(K * N) |> matrix(K, N)
  x <- sweep(x, 1, rowSums(x) / N, "-")
  x[, 1] <- x[, 1] - rowSums(x)
  x
}

K1 <- 3
K2 <- 2
```

```

N <- 4
costm <- cost_matrix_lp(1:N)

set.seed(123)
mu <- rsum0(K1, N)
nu <- rsum0(K2, N)

print(ot_cost_sgn(mu[2, ], nu[2, ], costm))

# mode = "diag" requires K1 = K2
print(ot_cost_sgn(mu[1:2, ], nu, costm, mode = "diag"))

print(ot_cost_sgn(mu, nu, costm))

# only works properly if costm is semi-metric
print(ot_cost_sgn(mu, NULL, costm))
# but it requires less computations than
print(ot_cost_sgn(mu, mu, costm))

```

ot_test_lp_solver	<i>Control FDOTT linear programming solver</i>
-------------------	--

Description

Create an object that controls the linear programming (LP) solver to use.

Usage

```
ot_test_lp_solver(name = NULL, ...)
```

Arguments

name	name of the LP solver.
...	optional control arguments passed to the corresponding LP solver.

Details

name can be any LP solver that is compatible with the ROI package infrastructure. In particular, the corresponding plugin package `ROI.plugin.name` must be installed. The default value corresponding to `name = NULL` can be set via `options(FDOTT.lp_solver = name)` (the default is "glpk").

Value

A `ot_test_lp_solver_control` object containing:

name	the name of the LP solver
control	list of control arguments passed to the LP solver

See Also

[ROI::ROI_available_solvers](#)

Examples

```
## Not run:
# glpk is already the default
options(FDOTT.lp_solver = "glpk")
## End(Not run)
# plugin needs to be installed, else we get error
if (requireNamespace("ROI.plugin.glpk")) {
  # add control parameter (specific to glpk)
  sol <- ot_test_lp_solver("glpk", verbose = TRUE)
  print(sol)
} else {
  cat("'ROI.plugin.glpk' needs to be installed!\n")
}
```

tab_sample

Generate tabulated samples from probability vectors

Description

Generate count vectors instead of samples, i.e., vectors giving the number of times a sample was observed at the respective points.

Usage

```
tab_sample(n, mu, prob = FALSE)
```

Arguments

n	vector or nested list of sample sizes.
mu	matrix (row-wise) or nested list containing probability vectors to sample from. The structure of n and mu must be the same.
prob	logical value indicating whether probabilities (instead of counts) should be returned.

Value

The count vectors corresponding to the generated samples. Has the same structure as mu.

Examples

```
## matrix example

mu <- matrix(c(0.01, 0.99, 0.5, 0.5), 2, 2, TRUE)
n <- c(80, 20)

set.seed(123)
cv <- tab_sample(n, mu)
print(cv)
# sample sizes are rowsums
print(rowSums(cv))
# empirical probability vectors
print(sweep(cv, 1, n, "/"))
set.seed(123)
# same result
print(tab_sample(n, mu, prob = TRUE))

## list example

mu <- list(
  list(c(0.3, 0.7), c(0.25, 0.75)),
  list(c(0, 1), c(0.5, 0.5))
)
n <- list(list(100, 120), list(80, 90))

set.seed(123)
cv <- tab_sample(n, mu)
print(cv)
# empirical probability vectors
print(rapply(cv, \(x) x / sum(x), how = "replace"))
set.seed(123)
print(tab_sample(n, mu, prob = TRUE))
```

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