

Package ‘cooltools’

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Type Package

Title Practical Tools for Scientific Computation and Visualisation

Version 2.33

Description Provides utilities for scientific computation and visualisation, with an emphasis on applications in physics and astrophysics. Functionality includes random sampling from spherical and custom distributions, information and entropy analysis, Fourier transforms, two-point correlation estimation, binning and gridding of point sets, two-dimensional interpolation, Monte Carlo integration, vector operations, coordinate transformations, physical constants, and cosmological conversions. Graphics tools support the creation and export of publication-quality plots, animations, colour scales, map projections, and bitmap images. Several of these tools were used by Obreschkow et al. (2020) <[doi:10.1093/mnras/staa445](https://doi.org/10.1093/mnras/staa445)>.

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cooltools-package

*Practical Tools for Scientific Computations and Visualizations***Description**

Collection of routines for efficient scientific computations in physics and astrophysics. These routines include utility functions, advanced computation tools, as well as visualisation tools. They can be used, for example, for generating random numbers from spherical and custom distributions, information and entropy analysis, special Fourier transforms, two-point correlation estimation (e.g. as in Landy & Szalay (1993) <doi:10.1086/172900>), binning & gridding of point sets, 2D interpolation, Monte Carlo integration, vector arithmetic and coordinate transformations. Also included are a non-exhaustive list of important constants and cosmological conversion functions. The graphics routines can be used to produce and export publication-ready scientific plots and movies, e.g. as used in Obreschkow et al. (2020) <doi:10.1093/mnras/staa445>. These routines include special color scales, projection functions, and bitmap handling routines.

Author(s)

Danail Obreschkow

See Also

Useful links:

- <https://github.com/obreschkow/cooltools>

.cooltools.env

*Package environment***Description**

Environment used to store global variables in the package, e.g. used for subplot routine.

Usage

.cooltools.env

Value

None

Author(s)

Danail Obreschkow

alp	<i>Associated Legendre Polynomials</i>
-----	--

Description

Compute associated Legendre polynomials $P_l^m(x)$, defined as the canonical solutions of the general Legendre equation. These polynomials are used, for instance, to compute the spherical harmonics.

Usage

```
alp(x, l = 0, m = 0)
```

Arguments

x	real argument between -1 and +1, can be a vector
l	degree of the polynomial (0,1,2,...); accurate to about 25
m	order of the polynomial (-l,-l+1,...,l); for negative values the standard convention is used: if $m > 0$, then $P(x,l,-m) = P(x,l,m) (-1)^m \text{factorial}(l-m) / \text{factorial}(l+m)$.

Value

Returns a vector with the same number of elements as x

Author(s)

Danail Obreschkow

See Also

[sphericalharmonics](#)

angularmomentum	<i>Compute the total angular momentum of a particle distribution</i>
-----------------	--

Description

Computes the total angular momentum of a set of particles about their centre of mass (or about a user-specified origin).

Usage

```
angularmomentum(m, x, v, x0 = NULL, v0 = NULL)
```

Arguments

<code>m</code>	<code>n</code> -vector or scalar of particle masses. For specific angular momentum computation, set <code>m=1</code> .
<code>x</code>	$n \times 3$ matrix of particle positions.
<code>v</code>	$n \times 3$ matrix of particle velocities.
<code>x0</code>	Optional 3-vector specifying the origin about which the angular momentum is computed. If NULL (default), the centre of mass is used.
<code>v0</code>	Optional 3-vector specifying the reference velocity. If NULL (default), the centre-of-mass velocity is used.

Value

A numeric vector of length three containing the Cartesian components of the total angular momentum,

$$\mathbf{J} = \sum_i m_i (\mathbf{x}_i - \mathbf{x}_0) \times (\mathbf{v}_i - \mathbf{v}_0).$$

If `m` is NULL, a vector of zeros is returned.

Examples

```
m = c(1, 2)
x = rbind(c(1, 0, 0), c(0, 1, 0))
v = rbind(c(0, 1, 0), c(-1, 0, 0))
angularmomentum(m, x, v)
```

approxfun2

Bilinear interpolation function of data on a regular grid

Description

Generates a fast function $f(x,y)$ that interpolates gridded data, based on the analogous subroutine [approxfun](#) in 1D.

Usage

```
approxfun2(x, y, z, outside = NA)
```

Arguments

<code>x</code>	<code>n</code> -vector of <code>x</code> -coordinates; must be strictly monotonically increasing, but not necessarily equally spaced
<code>y</code>	<code>m</code> -vector of <code>y</code> -coordinates; must be strictly monotonically increasing, but not necessarily equally spaced
<code>z</code>	<code>n</code> -by- <code>m</code> matrix containing the known function values at the (x,y) -coordinates
<code>outside</code>	value of the approximation function outside the grid (default is NA)

Value

Returns a fast and vectorized interpolation function $f(x,y)$

Author(s)

Danail Obreschkow

See Also

[approxfun](#)

Examples

```
x = seq(3)
y = seq(4)
z = array(c(x+1,x+2,x+3,x+4),c(3,4))
f = approxfun2(x,y,z)
print(f(1.7,2.4))
```

bindata	<i>Bin two-dimensional data in one dimension</i>
---------	--

Description

Divides a vector of values x into finite intervals; returns the counts and other statistics in each interval.

Usage

```
bindata(x, y = NULL, bins = 20, method = "regular", xlim = NULL)
```

Arguments

x	N-element vector of x-coordinates
y	optional N-element vector of values associated with the different points in x
bins	If method is 'regular' or 'equal', this is a scalar specifying the number of bins. If method is 'custom' this is a vector of (n+1) x-values delimiting the n bins.
method	Character string. Choose 'regular' for regularly space bins, 'equal' for bins containing an equal number of points (+-1), or 'custom' for bins with custom edges.
xlim	optional 2-element vector specifying the data range (data cropped if necessary). If not given, xlim is set to the full range of x.

Value

Returns a list of items

<code>n</code>	number of bins
<code>xlim</code>	considered range of x-coordinates, same as input argument <code>xlim</code> , if given
<code>xleft</code>	n-element vector containing the x-coordinates of the left bin edges
<code>xmid</code>	n-element vector containing the x-coordinates of the bin centres
<code>xright</code>	n-element vector containing the x-coordinates of the right bin edges
<code>dx</code>	n-element vector containing the widths of the bins
<code>count</code>	n-element vector containing the number of points in each bin
<code>x</code>	n-element vector containing the mean x-values in each bin
<code>y</code>	n-element vector containing the mean y-values in each bin
<code>xmedian</code>	n-element vector containing the median of the x-values in each bin
<code>ymedian</code>	n-element vector containing the median of the y-values in each bin
<code>yerr</code>	n-element vector giving the uncertainty on the mean
<code>ysd</code>	n-element vector giving the standard deviations of the y-values
<code>y16</code>	n-element vector giving the 15.86-percentile of the y-values
<code>y84</code>	n-element vector giving the 84.13-percentile of the y-values

Author(s)

Danail Obreschkow

See Also

[griddata](#)

Examples

```
# make and plot 100 random (x,y)-points
set.seed(1)
x = runif(200)
y = x+rnorm(200)
plot(x,y,pch=16,cex=0.5)

# bin the data into 10 bins of 20 points each
bin = bindata(x,y,10,'equal')
segments(bin$xleft,bin$y,bin$xright,bin$y,col='red')
segments(bin$x,bin$y16,bin$x,bin$y84,col='red')
segments(bin$x,bin$y-bin$yerr,bin$x,bin$y+bin$yerr,col='red',lwd=3)
points(bin$x,bin$y,pch=16,col='red')
```

blur*Gaussian blur for arrays of arbitrary dimension*

Description

Smooth a numeric array of arbitrary dimension with a separable Gaussian kernel. This function is conceptually similar to `gblur` from the **EBImage** package (which is limited to 2D), but works for arrays of any dimension.

Usage

```
blur(x, sigma, boundary = "replicate")
```

Arguments

<code>x</code>	A numeric array to be smoothed.
<code>sigma</code>	A non-negative numeric scalar or numeric vector specifying the standard deviation(s) of the Gaussian kernel in pixel units. If a single value is provided, it is used for all dimensions.
<code>boundary</code>	A character string specifying the boundary handling, or a character vector of length equal to the number of dimensions of <code>x</code> . Possible values are <code>"none"</code> , <code>"circular"</code> , and <code>"replicate"</code> . If a single value is provided, it is used for all dimensions.

Details

The Gaussian kernel is separable, so smoothing is performed via successive 1D convolutions along each dimension.

This function is similar in spirit to `gblur` from **EBImage**, but generalises naturally to arrays of arbitrary dimension.

Boundary handling can be controlled via `'boundary'`:

- `"none"` uses centered filtering without padding and therefore returns `'NA'` values near array boundaries.
- `"circular"` applies periodic wrap-around boundary conditions.
- `"replicate"` extends the array by repeating the edge values.

For finite arrays, the Gaussian kernel is truncated as needed so that its length does not exceed the array extent along any dimension.

Value

A numeric array with the same dimensions as `x`, containing the blurred values.

car2pol

Cartesian to polar/cylindrical coordinate conversion

Description

Convert 2D/3D Cartesian to polar/cylindrical coordinates

Usage

car2pol(x)

Arguments

x 2/3-vector or n-by-2/3 matrix representing the Cartesian components x,y,(z) of n two/three-dimensional vectors

Value

Returns a 2/3-vector or a n-by-2/3 matrix representing the polar/cylindrical coordinates r,phi,(z), where phi=0...2*pi is the azimuth measured positively from the x-axis.

Author(s)

Danail Obreschkow

See Also

[pol2car](#)

car2sph*Cartesian to spherical coordinate conversion*

Description

Convert 3D Cartesian to spherical coordinates

Usage

car2sph(x)

Arguments

x 3-vector or n-by-3 matrix representing the Cartesian components (x,y,z) of n three-dimensional vectors

Value

Returns a 3-vector or a n-by-3 element matrix representing the spherical coordinates (r,theta,phi), where theta=0...pi is the polar angle measured from the north pole and phi=0...2*pi is the azimuth measured positively from the x-axis (ISO 80000-2:2019 physics convention).

Author(s)

Danail Obreschkow

See Also

[sph2car](#)

cmplx2col	<i>Convert complex numbers to color</i>
-----------	---

Description

Converts a complex number (or a vector/array thereof) into a color-string, such that brightness represents the complex amplitude and hue represents the complex phase.

Usage

```
cmplx2col(z, max = NULL, hue = 0, saturation = 1, gamma = 1)
```

Arguments

z	complex number or vector/array of complex numbers
max	value of the complex module that corresponds to full brightness; if not given, this is set equal to the maximum complex amplitude in z.
hue	hue value of positive reals
saturation	saturation value of colors
gamma	positive number to adjust the non-linearity of the color scale (1=linear)

Value

Returns a single color or vector/array of colors

Author(s)

Danail Obreschkow

colorbar	<i>Vertical color bar</i>
----------	---------------------------

Description

Adds a vertical color bar to a plot with a custom axis.

Usage

```
colorbar(
  xleft,
  ybottom,
  xright,
  ytop,
  col = gray.colors(256, 0, 1),
  clim = c(0, 1),
  show.border = TRUE,
  text = "",
  line = 2,
  show.axis = TRUE,
  side = "right",
  lwd = 1,
  nticks = 5,
  at = NULL,
  srt = 0,
  ticklength = 0.1,
  shift = 0,
  ...
)
```

Arguments

xleft	left x-coordinate of the bar
ybottom	bottom y-coordinate of the bar
xright	right x-coordinate of the bar
ytop	top y-coordinate of the bar
col	vector of colors
clim	2-vector specifying the range of values, linearly represented by the full color scale
show.border	logical flag specifying whether to draw a rectangular border around the bar
text	axis label
line	distance between label and color bar
show.axis	logical flag specifying whether to draw an axis

side	character string, which specifies the location of the axis on the bar. This has to be 'left' or 'right' (default).
lwd	linewidth of border and ticks
nticks	number of ticks on the axis
at	vector of values specifying the tick positions on the axis, this overrides nticks.
srt	rotation angle of tick text
ticklength	length of ticks
shift	extra distance between axis numbers and color bar
...	optional arguments to be passed text function.

Value

None

Author(s)

Danail Obreschkow

Examples

```
## Plot a spherical function with color bar
nplot(xlim=c(0,1.2), asp=1)
f = function(theta,phi) cos(10*theta+phi)
sp = sphereplot(f, 200, col=planckcolors(200), phi0=0.1, theta0=pi/3,
add=TRUE, center=c(0.5,0.5), radius=0.4, clim=c(-1,1))
colorbar(1,0.1,1.1,0.9,col=sp$col,clim=sp$clim)
```

contourlevel	<i>Highest-density contour levels</i>
--------------	---------------------------------------

Description

Computes density thresholds defining highest-density regions.

For each probability p , the function returns a level ℓ such that the region where the density is at least ℓ contains a fraction p of the total probability mass:

$$\frac{\int_{f(\mathbf{x}) \geq \ell} f(\mathbf{x}) d\mathbf{x}}{\int f(\mathbf{x}) d\mathbf{x}} = p.$$

The input may be a numeric vector or array containing sampled density values, or a function representing a density over a bounded rectangular domain. The density does not need to be normalised, but it must be non-negative and have a finite, positive integral or sum.

Usage

```

contourlevel(
  f,
  p = c(0.6826895, 0.9544997),
  xmin = NULL,
  xmax = NULL,
  neval = 10000,
  subdivisions = 1000,
  napprox = 30,
  rel.tol = 1e-05,
  abs.tol = 0,
  ...
)

```

Arguments

<code>f</code>	A non-negative numeric vector or array, or a function of a numeric vector. If <code>f</code> is a function, it must return a single finite, non-negative density value.
<code>p</code>	Numeric vector of enclosed probability masses. Every value must lie strictly between 0 and 1.
<code>xmin, xmax</code>	Numeric vectors giving the lower and upper limits of the integration domain. These arguments are required when <code>f</code> is a function and must have equal lengths. Outside this rectangular domain, <code>f</code> is assumed to be zero.
<code>neval</code>	Positive integer giving the maximum number of function evaluations used in each multidimensional numerical integration.
<code>subdivisions</code>	Positive integer giving the maximum number of subintervals used by integrate in one dimension.
<code>napprox</code>	Number of trial density levels used to interpolate the enclosed-mass function when <code>f</code> is a function. Larger values are generally more accurate but require more numerical integrations. If <code>napprox=0</code> , each requested contour level is determined directly by root-finding.
<code>rel.tol</code>	Positive relative tolerance used for numerical integration.
<code>abs.tol</code>	Non-negative absolute tolerance used for numerical integration.
<code>...</code>	Additional arguments passed to <code>f</code> .

Details

The returned contours define highest-density regions: points are included in decreasing order of density until the requested probability mass is enclosed. For multimodal densities, the resulting region may consist of several disconnected components.

When `f` is a function, the enclosed mass above a trial level is evaluated by numerically integrating

$$f(\mathbf{x})I[f(\mathbf{x}) \geq \ell].$$

This integrand is discontinuous at the contour boundary, so convergence may be slower than for a smooth integrand, particularly in high dimensions or for complicated contours.

One-dimensional densities are integrated using [integrate](#). Multidimensional densities are integrated using [cuhre](#).

If `napprox>0`, the enclosed-mass function is evaluated on a grid of density levels and inverted by monotonic linear interpolation. If `napprox=0`, each requested probability is solved separately using [uniroot](#). The latter is generally slower but avoids the interpolation approximation.

Value

A numeric vector of density levels with the same length and ordering as `p`.

For a vector or array, all entries are assumed to represent cells of equal volume or equal statistical weight. Because the enclosed mass changes in discrete steps, the returned level is the sampled density threshold whose superlevel set first contains at least the requested probability mass.

Author(s)

Danail Obreschkow

See Also

[dpqr](#)

Examples

```
## f(x) is a one-dimensional PDF
# Compute the one- and two-sigma contour levels of a normal distribution,
# i.e. the values l such that
# integral over dnorm(x) >= l of dnorm(x) dx = p,
# where p = 68.3% and 95.4%.
l = contourlevel(dnorm, xmin = -10, xmax = 10, napprox = 0)
print(l)

# Compare these values with dnorm(1) and dnorm(2)
print(dnorm(c(1, 2)))

## f(x) is a two-dimensional likelihood function
# Produce 20%, 40%, 60%, and 80% highest-density contours.
f = function(x) {
  cos(2*x[1]-x[2]-1)^2*exp(-x[1]^2-x[2]^2-x[1]*x[2])
}

p = c(0.2, 0.4, 0.6, 0.8)

# Values l such that
# integral over f(x) >= l of f(x) dx = p * integral f(x) dx
l = contourlevel(f, p, c(-5, -5), c(5, 5))

# Plot the function and contours at the levels l
x = seq(-3, 3, length.out = 200)
m = pracma::meshgrid(x)
z = array(Vectorize(function(x, y) f(c(x, y)))(m$Y, m$X), dim(m$X))
```

```

image(x, x, z, col = terrain.colors(100))
contour(x, x, z, levels = 1, add = TRUE,
        labels = sprintf("%.0f%%", p*100), labcex = 0.7)

## f is a 20-by-20 array representing a gridded point set
# Produce 1000 points drawn from a two-dimensional normal distribution.
set.seed(1)
x = MASS::mvrnorm(n = 1000, mu = c(0, 0), Sigma = matrix(c(3, 1, 1, 2), 2, 2))

# Grid these points onto a regular 20-by-20 grid
g = griddata(x, min = -6, max = 6)

# Find one- and two-sigma contour levels and draw the contours
l = contourlevel(g$field)

plot(x, xlim = g$grid[[1]]$lim, ylim = g$grid[[2]]$lim, pch = 20, cex = 0.5)
contour(g$grid[[1]]$mid, g$grid[[2]]$mid, g$field,
        levels = l, add = TRUE, col = "red", lwd = c(2, 1), labels = NA)

```

cosmofct

Fast cosmology conversion functions

Description

Generates all 20 conversion functions between redshift (z), luminosity distance (dl), comoving distance (dc) and angular diameter distance (da), and lookback time (t = light travel time from specified redshift); based on the **celestial** package.

Usage

```
cosmofct(zmin = 0, zmax = 1, dz = 0.02, H0 = 70, OmegaM = 0.3, ...)
```

Arguments

<code>zmin</code>	minimum redshift for which the conversion functions are used
<code>zmax</code>	maximum redshift for which the conversion functions are used
<code>dz</code>	redshift interval on which the conversion functions are interpolated (default of 0.02 is normally largely sufficient)
<code>H0</code>	local Hubble constant in units of km/s/Mpc (default 70).
<code>OmegaM</code>	local normalised matter density (default 0.3).
<code>...</code>	other cosmological parameters accepted by <i>cosdist</i> of the <i>*celestial*</i> package. Defaults are $\Omega_L = 1 - \Omega_M - \Omega_R$, $\Omega_R = 0$, $w_0 = -1$, $w_{\text{prime}} = 0$.

Value

Returns a list of 20 vectorized functions; e.g. `dc2z` to convert from comoving distance to redshift. Also contains the age of the universe at $z=0$. All distances are in units of Mpc and times are in units of Gyr.

Author(s)

Danail Obreschkow (based on `*celestial*` package by Aaron Robotham)

Examples

```
## uses a flat LCDM cosmology with h=0.68, OmegaM=0.32 and OmegaL=0.68
cosmo = cosmoft(0,1,H0=68,OmegaM=0.32)
curve(cosmo$z2dl(x),0,1,xlab='z',ylab='distance',col='red')
curve(cosmo$z2dc(x),0,1,col='black',add=TRUE)
curve(cosmo$z2da(x),0,1,col='blue',add=TRUE)
d = seq(500,5000,500)
points(cosmo$dl2z(d),d,pch=16,col='red')
points(cosmo$dc2z(d),d,pch=16,col='black')
points(cosmo$da2z(d),d,pch=16,col='blue')
```

cshift

Circularly shift each dimension of an array

Description

Circulates each dimension of an array. This routine is identical to [circshift](#), but works with arrays up to 5 dimensions.

Usage

```
cshift(x, s)
```

Arguments

<code>x</code>	vector or array (up to rank 5)
<code>s</code>	scalar, if <code>x</code> is a vector, or a vector of length matching the rank of <code>x</code> , if <code>x</code> is an array

Value

Returns a vector or array of the same shape as `x`.

Author(s)

Danail Obreschkow

cst	<i>Scientific constants</i>
-----	-----------------------------

Description

The list `cst` contains useful scientific constants in SI units, mainly for astrophysics.

Usage

`cst`

Value

None

Author(s)

Danail Obreschkow

Examples

```
# print all the constants to console
for (i in seq(length(cst))) cat(sprintf('%6s = %.12e\n',names(cst)[i],cst[i]))
```

cubehelix	<i>Cube Helix colour palette</i>
-----------	----------------------------------

Description

Generate the Cube Helix colour palette, designed to appropriately display of intensity images, as the brightness increases monotonically when displayed in greyscale.

Usage

```
cubehelix(n, r = 1.5, hue = 1, gamma = 1, rev = FALSE)
```

Arguments

<code>n</code>	integer number of colours in the scale
<code>r</code>	real number specifying the number of rotations of the helix over the scale
<code>hue</code>	non-negative number specifying the colour intensity from grey (0) to normal (1) and over-saturated (>1)
<code>gamma</code>	positive number specifying the relative importance of low vs high values
<code>rev</code>	logical flag indicating whether the ordering of the colors should be reversed

Details

This scheme was published by Green, D. A., 2011, "A colour scheme for the display of astronomical intensity images." Bulletin of the Astronomical Society of India, 39, 289.

Value

Returns an n-vector of RGB colour strings.

Author(s)

Danail Obreschkow

dft	<i>Discrete Fourier Transform</i>
-----	-----------------------------------

Description

Discrete Fourier Transform (DFT) with longest modes at the center in Fourier space and normalized such that $\text{dft}(\text{dft}(f), \text{inverse}) = f$. This is the discretization scheme described in Appendix D of Obreschkow et al. 2013, ApJ 762. Relies on [fft](#).

Usage

```
dft(f, inverse = FALSE, shift = -floor(dim(as.array(f))/2), simplify = TRUE)
```

Arguments

<code>f</code>	real or complex D-dimensional array containing the values to be transformed.
<code>inverse</code>	logical flag; if TRUE the inverse Fourier transform is performed.
<code>shift</code>	D-vector specifying the integer shift of the coordinates in Fourier space. Set to <code>shift=rep(0,D)</code> to produced a DFT with the longest mode at the corner in Fourier space.
<code>simplify</code>	logical flag; if TRUE the complex output array will be simplified to a real array, if it is real within the floating point accuracy

Value

Returns an array of the same shape as `f`, containing the (inverse) Fourier Transform.

Author(s)

Danail Obreschkow

See Also

[fft](#)

Examples

```
## DFT of a 2D normal Gaussian function
n = 30
f = array(0,c(n,n))
for (i in seq(n)) {
  for (j in seq(n)) f[i,j] = exp(-(i-6)^2/4-(j-8)^2/2-(i-6)*(j-8)/2)
}
plot(NA,xlim=c(0,2.1),ylim=c(0,1.1),asp=1,bty='n',xaxt='n',yaxt='n',xlab='',ylab='')
rasterImage(f,0,0,1,1,interpolate=FALSE)
g = dft(f)
img = array(hsv((prasma::angle(g)/2/pi)%1,1,abs(g)/max(abs(g))),c(n,n))
rasterImage(img,1.1,0,2.1,1,interpolate=FALSE)
text(0.5,1,'Input function f',pos=3)
text(1.6,1,'DFT(f)',pos=3)
```

dftgrid

Produce coordinates for Discrete Fourier Transform

Description

Produces the direct space coordinates (x) and Fourier space frequencies (f) and angular frequencies (k), corresponding to the Discrete Fourier Transform `dft` of this package.

Usage

```
dftgrid(N, L, x0 = 0, k0 = -floor(N/2) * 2 * pi/L)
```

Arguments

N	number of divisions along one dimension used in direct and Fourier space
L	side-length (=period) of the data long one dimension
x0	zero-point of x-coordinates (=0 in most applications)
k0	zero-point of k-coordinates (=0 or $-\text{floor}(N/2) \cdot dk$ in most applications)

Value

Returns a list with:

x	vector of direct space coordinates
f	vector of Fourier space coordinates (frequencies)
k	vector of Fourier space coordinates (angular frequencies)
dx	spacing of x-values
df	spacing of f-values
dk	spacing of k-values
L	input value of L
N	input value of N

Author(s)

Danail Obreschkow

distradius	<i>Radius of a point distribution</i>
------------	---------------------------------------

Description

Computes a characteristic radius of a set of points about a centre.

Usage

```
distradius(x, m = NULL, x0 = NULL, type = c("max", "mean", "median"))
```

Arguments

x	Numeric vector or matrix. If a matrix is supplied, each row is interpreted as a point.
m	Optional numeric vector of point masses or weights. If NULL, equal weights are used.
x0	Optional numeric vector specifying the centre. If NULL, the weighted centre of mass is used.
type	Character string specifying the radius definition. One of "max", "mean" or "median".

Value

A scalar radius.

See Also

[vectornorm](#)

dpqr	<i>Generate the d/p/q/r family for an arbitrary distribution</i>
------	--

Description

Generates the standard d, p, q, and r functions associated with an arbitrary one-dimensional probability density function, analogous to dnorm/pnorm/qnorm/rnorm and related families.

Usage

```
dpqr(fun, min, max)
```

Arguments

<code>fun</code>	A non-negative, vectorised function proportional to a probability density. It does not need to be normalised.
<code>min, max</code>	Lower and upper bounds of the support. The density is assumed to be zero outside this interval.

Value

Returns a list with the following functions:

<code>d(x)</code>	Probability density function (PDF), i.e. a normalised version of <code>fun</code> on the domain <code>[min, max]</code> .
<code>p(x)</code>	Cumulative distribution function (CDF).
<code>q(p)</code>	Quantile function.
<code>r(n)</code>	Generates <code>n</code> random samples from the distribution.

Author(s)

Danail Obreschkow

See Also

[rng](#), [contourlevel](#)

Examples

```
f = function(x) sin(x)
dist = dpqr(f, 0, pi)

x = dist$r(1000)
hist(x, probability = TRUE)
curve(dist$d(x), add = TRUE)
```

entropy

Information entropy

Description

Computes the information entropy $H = -\sum(p \cdot \log_b(p))$, also known as Shannon entropy, of a probability vector `p`.

Usage

```
entropy(p, b = exp(1), normalize = TRUE)
```

Arguments

p	vector of probabilities; typically normalized, such that $\text{sum}(p)=1$.
b	base of the logarithm (default is e)
normalize	logical flag. If TRUE (default), the vector p is automatically normalized.

Value

Returns the information entropy in units that depend on b. If $b=2$, the units are bits; if $b=\exp(1)$, the units are nats; if $b=10$, the units are dits.

Author(s)

Danail Obreschkow

errlines	<i>Draw a line with uncertainty regions</i>
----------	---

Description

Draw a line with uncertainty regions

Usage

```
errlines(
  x,
  y,
  errp,
  errn = errp,
  col = "black",
  alpha = 0.5,
  smooth = FALSE,
  df = NULL,
  ...
)
```

Arguments

x	vector of x-coordinates
y	vector of y-coordinates
errp	vector of y-errors in the positive direction (upwards)
errn	vector of y-errors in the negative direction (downwards)
col	color of the line
alpha	transparency of the uncertainty region
smooth	logical flag indicating whether the line should be smoothed
df	df (=degrees of freedom) parameter of smooth.spline function
...	additional parameters used by lines

Value

None

Author(s)

Danail Obreschkow

error

Stop code and produce an error message

Description

Stops the code and produces an error message, like the `stop()` function of the base library, but terminating a timer started with `tick`, if running.

Usage

```
error(...)
```

Arguments

... zero or more objects which can be coerced to character (and which are pasted together with no separator) or a single condition object.

Value

None. `geterrmessage()` returns the last error message, as a character string.

Author(s)

Danail Obreschkow

See Also

[tick](#) [tock](#) [progress](#)

fibonaccisphere	<i>Evenly distributed n points on a sphere</i>
-----------------	--

Description

Distributes n points on a sphere in a relatively even fashion following the generalised Fibonacci algorithm, described at <http://extremelearning.com.au/evenly-distributing-points-on-a-sphere/>

Usage

```
fibonaccisphere(n = 1000, r = 1, out.xyz = TRUE, out.sph = FALSE)
```

Arguments

n	number of points to be placed on the sphere
r	radius
out.xyz	logical flag specifying whether to return Cartesian coordinates (default is TRUE)
out.sph	logical flag specifying whether to return spherical coordinates (default is FALSE); theta=colatitude (=polar angle=angle from z-axis), phi=longitude (=azimuth angle),

Value

matrix of n points (in n rows), in Cartesian and/or spherical coordinates.

Author(s)

Danail Obreschkow

See Also

[runif3](#)

Examples

```
## plot standard projections of a 1000-point Fibonacci sphere
xyz = fibonaccisphere()
plot(xyz, asp=1, pch=16, cex=0.5)
```

getgit

Install a GitHub Package

Description

Installs an R package from GitHub using `pak::pak()`. If installation fails with GitHub HTTP error 401 / bad credentials, the stored GitHub credentials are deleted using `gitcreds::gitcreds_delete()`, and the installation is attempted once more.

Usage

```
getgit(reponame, ...)
```

Arguments

reponame	Character string. GitHub repository name in the form "owner/repo", e.g. "obreschkow/cooltools".
...	Additional arguments passed to <code>pak::pak()</code> .

Value

Invisibly returns the result of `pak::pak()`.

Examples

```
## Not run:
getgit("obreschkow/cooltools")

## End(Not run)
```

gradient

Compute gradient

Description

Evaluates the gradient of a vector of array of rank 2 or 3

Usage

```
gradient(f, circular = FALSE)
```

Arguments

f	vector or array of rank 2 or 3
circular	logical scalar or vector specifying whether periodic boundaries are used along each dimension

Value

returns a list with the different components of the gradient; each component has the same dimension as f.

Author(s)

Danail Obreschkow

grf

Gaussian Random Field generator

Description

Generates a scalar Gaussian Random Field (GRF) in 1, 2 or 3 dimensions, with a power-law power spectrum of custom slope alpha. The field is normalized such that its mean is zero (up to floating point errors) and its expected standard deviation is one, for alpha=0. The Fourier phases are sampled in order of increasing frequency, such that the random structure is preserved when changing the output size.

Usage

```
grf(nside = 100, dim = 2, alpha = 0, seed = NULL)
```

Arguments

nside	integer number of elements per dimension in the output matrix
dim	integer number of dimensions
alpha	spectral index, such that Fourier amplitudes scale as k^α . alpha=0 corresponds to uncorrelated white noise, alpha<0 is red noise, while alpha>1 is blue noise.
seed	optional seed for random number generator

Value

Returns a vector, matrix or 3D-array with nside elements per dimension

Author(s)

Danail Obreschkow

Examples

```
# Generate the same 2D GRF in two different resolutions
nplot(c(0,2.1), asp=1)
lowres = grf(inside=30, alpha=-2, seed=1)
graphics::rasterImage(stretch(lowres),0,0,1,1)
highres = grf(inside=120, alpha=-2, seed=1)
graphics::rasterImage(stretch(highres),1.1,0,2.1,1)

# Check the power spectrum of a general GRF
inside = 50 # change this to any integer >1
alpha = -1.7 # change this to any power
dim = 3 # change this to any positive integer (but keep inside^dim reasonable)
x = grf(inside=inside, dim=dim, alpha=alpha)
fourier.grid = dftgrid(N=inside,L=1)
knorm = vectornorm(expand.grid(rep(list(fourier.grid$k),dim)))
power = abs(dft(x))^2
b = bindata(knorm,power,method='equal')
plot(b$xmedian,b$ymedian,log='xy',pch=16,
      xlab='Fourier mode |k|',ylab='Power p(k)',main='Power spectrum')
graphics::curve(x^alpha/inside^dim,col='blue',add=TRUE) # expected power-law
```

griddata

Distribute a point set onto a regular grid

Description

Distributes a set of points in D dimensions onto a regular, D-dimensional grid, using a fast nearest-neighbor algorithm. Weights can be used optionally.

Usage

```
griddata(
  x,
  w = NULL,
  n = 10,
  min = NULL,
  max = NULL,
  type = c("counts", "density", "probability", "mean")
)
```

Arguments

x	N-element vector (if D=1) or N-by-D matrix (if D>1), giving the Cartesian coordinates of N points in D dimensions.
w	optional N-element vector with weights.
n	scalar or D-element vector specifying the number of equally spaced grid cells along each dimension.

min	optional scalar or D-element vector specifying the lower bound of the grid. If not given, min is adjusted to the range of x.
max	optional scalar or D-element vector specifying the upper bound of the grid. If not given, max is adjusted to the range of x.
type	character string specifying the normalization of the output. Must be one of: • "counts": returns the number of points in each cell, or the sum of weights if w is given. Thus the total number of points (or total mass, if weights are given) is <code>sum(field)</code>. • "density": returns the density, such that the total number of points (or total mass, if weights are given) is <code>sum(field) * dV</code>. • "probability": returns a probability density, such that <code>sum(field) * dV = 1</code>. • "mean": returns the mean weight in each cell. This option requires w to be given. Cells with no data are assigned NA.

Value

Returns a list of items

field	D-dimensional array representing the value in each grid cell. See parameter type for more details.
grid	List of D elements with the grid properties along each dimension: n = number of grid cells; mid = n-vector of mid-cell coordinates; breaks = (n+1)-vector of cell edges; min, max = considered range; delta = cell width.
dV	Single number representing the volume of the D-dimensional grid cells.

Author(s)

Danail Obreschkow

Examples

```
# On some machines data.table does not perform well in multi-threading mode.
# The following command limits this to one thread as a precaution, but
# may not be needed on most machines.
data.table::setDTthreads(1L)

# Distribute 1-dimensional data onto a regular grid
npoints = 1e4
x = rnorm(npoints)
g = griddata(x,min=-3,max=3,n=100,type='probability')
curve(dnorm(x),-3,3)
points(g$grid$mid,g$field,pch=16)

# Distribute 2-dimensional data onto a regular grid
x = runif(100,max=2)
y = runif(100)
g = griddata(cbind(x,y),min=c(0,0),max=c(2,1),n=c(20,10))
image(g$grid[[1]]$breaks,g$grid[[2]]$breaks,g$field,
```

```

      asp=1,col=grey.colors(100,0,1),xlab='x',ylab='y')
points(x,y,col='red',pch=16)

# ... same with weights
w = runif(100)
g = griddata(cbind(x,y),w,min=c(0,0),max=c(2,1),n=c(20,10))
image(g$grid[[1]]$breaks,g$grid[[2]]$breaks,g$field,
      asp=1,col=grey.colors(100,0,1),xlab='x',ylab='y')
points(x,y,col='red',pch=16,cex=w)

# ... mean weight in each cell (dark red, where no data)
par(bg = "darkred")
g = griddata(cbind(x,y),w,min=c(0,0),max=c(2,1),n=c(20,10),type='mean')
image(g$grid[[1]]$breaks,g$grid[[2]]$breaks,g$field,
      asp=1,col=grey.colors(100,0,1),xlab='x',ylab='y')
points(x,y,col='red',pch=16,cex=w)

```

histcoord

Generate histogram coordinates from mid points

Description

Converts the mid-point x-values and mean densities of binned data into (x,y)-coordinates of a histogram.

Usage

```
histcoord(x, y, yleft = 0, yright = 0)
```

Arguments

x	n-vector giving the bin mid-points
y	n-vector giving bin values
yleft	optional value specifying the value at the left edge
yright	optional value specifying the value at the right edge

Value

(2n+2)-by-2 matrix of (x,y)-coordinates to draw histogram as a connected line

Author(s)

Danail Obreschkow

Examples

```
x = seq(5)
y = sin(x)
plot(x,y,xlim=c(0,6))
lines(histcoord(x,y))
```

inertia

*Moment of inertia tensor***Description**

Computes the moment of inertia tensor of a set of point masses in arbitrary dimensions,

$$\mathbf{I} = \sum_i m_i (|\mathbf{x}_i|^2 \mathbf{1} - \mathbf{x}_i \mathbf{x}_i^T),$$

where $\mathbf{1}$ is the identity matrix.

Usage

```
inertia(x, m = 1)
```

Arguments

<code>x</code>	Numeric vector or matrix. If a matrix is supplied, each row is interpreted as a point.
<code>m</code>	Numeric scalar or vector of point masses. If a scalar is supplied, the same mass is assigned to every point.

Value

A symmetric $d \times d$ matrix containing the moment of inertia tensor, where d is the dimension of the points.

See Also

[moments](#), [quadrupole](#)

invert

Invert and shift colors of an image

Description

Invert the brightness of each color channel in an image and/or circularly shifts the hue value. Optionally, a Gaussian blur can be applied.

Usage

```
invert(
  img = NULL,
  invert = TRUE,
  colshift = 0,
  blur = 0,
  file.in = "",
  file.out = "",
  format = "png",
  show.image = TRUE
)
```

Arguments

<code>img</code>	n-by-m-by-3 array or n-by-m-by-4 array representing an rgb(+alpha) image
<code>invert</code>	logical flag indicating whether the channel-brightness should be inverted
<code>colshift</code>	numerical value between 0 and 1 setting the circular shift of the hue value. If <code>invert=TRUE</code> , choosing <code>colshift=0.5</code> preserves the colors, while inverting black and white.
<code>blur</code>	numerical value ≥ 0 defining the standard deviation of an optional Gaussian blur.
<code>file.in</code>	optional input filename, which can be used to load an image instead of providing it via <code>img</code> . This filename is ignored if <code>img</code> is specified.
<code>file.out</code>	optional output filename.
<code>format</code>	one of "png" or "jpg" specifying the file format of the input and output image.
<code>show.image</code>	logical flag specifying whether the image is displayed in the R console.

Value

Returns an n-by-m-by-3 array or n-by-m-by-4 array of the processed image.

Author(s)

Danail Obreschkow

Examples

```
img = yinyangyong # this is an example image included in the package

# invert brightness of all channels
invert(img)

# invert brightness, but preserve hue
invert(img, colshift=0.5)
```

is.equal

*Numerical equality check***Description**

Checks if two or more numerical values are identical within a relative numerical tolerance

Usage

```
is.equal(x, ..., stoptext = NULL, eps = sqrt(.Machine$double.eps))
```

Arguments

x	vector or array of values to compare
...	optional additional values to compare
stoptext	optional character string; if given, the routine stops if the values are not all equal and adds the character string to the error message
eps	relative numerical tolerance

Value

Returns a logical value. TRUE means that all values of x are equal within the specified relative tolerance; also returns TRUE if all values are Inf or NA or NaN.

Author(s)

Danail Obreschkow

Examples

```
# almost identical values
x = c(acos(1/sqrt(2)),pi/4)
print(x)
print(x[1]==x[2])
print(is.equal(x))

# various other examples
print(is.equal(1,2,3))
```

```

print(is.equal(1,NA,3))
print(is.equal(Inf,NA))
print(is.equal(NaN,NA))
print(is.equal(NaN,Inf))
print(is.equal(Inf,Inf,Inf))
print(is.equal(NA,NA))
print(is.equal(NaN,NaN))
print(is.equal(1.4,1.4))
print(is.equal(1.4,1.400000001))
print(is.equal(1.4,1.400000001,1.41))
print(is.equal(0,0,0,0))

```

jackknife

Jackknife Estimation

Description

Computes the "leave-one-out" Jackknife bias and standard error of an estimator $f(x)$ of a data-vector x , or an estimator $f(x,y)$ of vectors x and y . See Efron and Tibshirani (1993) for details

Usage

```
jackknife(x, f, y = NULL, ...)
```

Arguments

<code>x</code>	data vector
<code>f</code>	estimator function $f(x, \dots)$ or $f(x,y, \dots)$
<code>y</code>	optional data vector if f is a function of two vectors, such as the correlation coefficient $\text{cor}(x,y)$.
<code>...</code>	optional arguments to be passed to f .

Value

Returns a list with the following components:

<code>value</code>	Default value of the estimator f .
<code>bias</code>	Jackknife bias estimate of f .
<code>unbiased</code>	Bias-corrected value of f .
<code>sd</code>	Jackknife standard error of f .

Author(s)

Danail Obreschkow

kappacorotation	<i>Compute the co-rotational kinetic energy fraction</i>
-----------------	--

Description

Computes the co-rotational kinetic energy fraction, κ_{co} , of a particle distribution. This quantity is defined as the fraction of the total kinetic energy invested in ordered co-rotation about the total angular momentum axis. It is commonly used as a measure of the rotational support of galaxies in particle-based simulations.

Usage

```
kappacorotation(m, x, v, x0 = NULL, v0 = NULL)
```

Arguments

m	n-vector of particle masses.
x	$n \times 3$ matrix of particle positions.
v	$n \times 3$ matrix of particle velocities.
x0	Optional length-3 vector specifying the origin. If NULL (default), the centre of mass is used.
v0	Optional length-3 vector specifying the reference velocity. If NULL (default), the centre-of-mass velocity is used.

Details

The rotation axis is taken to be the direction of the total angular momentum of the particle distribution after subtracting the centre-of-mass position and velocity. Only particles with positive angular momentum about this axis contribute to the co-rotational kinetic energy.

Value

A scalar in the range $[0, 1]$ giving the fraction of the total kinetic energy contained in co-rotating azimuthal motion,

$$\kappa_{\text{co}} = \frac{\sum_{j_z > 0} m v_\phi^2}{\sum m |\mathbf{v}|^2},$$

where j_z is the specific angular momentum about the total angular momentum axis and $v_\phi = j_z/R$ is the azimuthal velocity. The common factor of $1/2$ in the kinetic energies cancels.

If m is NULL, NA is returned.

See Also

[angularmomentum #'](#)

Examples

```

m <- rep(1, 100)
x <- matrix(rnorm(300), ncol = 3)
v <- matrix(rnorm(300), ncol = 3)
kappacorotation(m, x, v)

```

kde2

Multi-dimensional adaptive kernel density estimation

Description

Produces a 2D kernel density estimation on a 2D grid from a D-dimensional ($D \geq 2$) point set

Usage

```

kde2(
  x,
  w = NULL,
  nx = 300,
  xlim = NULL,
  ylim = NULL,
  smoothing = 1,
  sigma = NULL,
  sigma.min = 0,
  sigma.max = Inf,
  reflect = "",
  algorithm = "kdenn",
  probability = FALSE
)

```

Arguments

x	N-by-D vector of x-coordinates or N-by-2 matrix of (x,y)-coordinates
w	optional N-element vector with weights
nx	integer specifying the number of equally spaced grid cells along the x-axis; the number ny of pixels along the y-axis is determined automatically from xlim and ylim.
xlim	2-element vector specifying the x-range
ylim	2-element vector specifying the y-range; if needed, this range is slightly adjusted to allow for an integer number of pixels.
smoothing	positive linear smoothing factor; the larger, the smoother the density field
sigma	optional N-vector, specifying the blurring of each pixel individually in length units of x; only used if algorithm=4.

<code>sigma.min</code>	optional value, specifying the minimum blurring of any pixel, expressed in standard deviations in length units of <code>x</code>
<code>sigma.max</code>	optional value, specifying the maximum blurring of any pixel, expressed in standard deviations in length units of <code>x</code>
<code>reflect</code>	vector of strings <code>c('left','right','bottom','top')</code> specifying the edges, where the data should be reflected to avoid probability density leaking outside the window
<code>algorithm</code>	integer value or character string specifying the smoothing algorithm: <code>basic (0)</code> : basic nearest-neighbor gridding algorithm without smoothing <code>blur (1)</code> : simple Gaussian blur of gridded density field <code>kdefast (2)</code> : 2D smoothing method that ignores higher dimensional information and applies a smoothing size to each pixel that depends on the number of objects in each pixel <code>kdenn (3)</code> : sophisticated Kernel density estimator that uses D-dimensional nearest neighbor separations to smooth each data point individually <code>manual (4)</code> : smooths each data point individually using a Gaussian Kernel with point-dependent standard deviations given in the optional vector <code>sigma</code>
<code>probability</code>	logical flag. If <code>TRUE</code> , the output field is normalized such that $\text{sum}(\text{field})\text{dpixel}^2=1$. If <code>FALSE</code> (default), the field is such that $\text{sum}(\text{field})\text{dpixel}^2$ equals the effective number of particles (or effective mass, if weights are given) in the range specified by <code>xlim</code> and <code>ylim</code> , including particle fractions that have been smoothed into the field and excluding particle fractions that have been smoothed out of it.

Value

Returns a list of items

<code>field</code>	2D array of smoothed density field.
<code>x</code>	<code>nx</code> -element vector of cell-center x-coordinates.
<code>y</code>	<code>ny</code> -element vector of cell-center y-coordinates.
<code>xbreak</code>	<code>(nx+1)</code> -element vector of cell-edge x-coordinates.
<code>ybreak</code>	<code>(ny+1)</code> -element vector of cell-edge y-coordinates.
<code>dpixel</code>	grid spacing along x-coordinate and y-coordinate.
<code>algorithm</code>	name of algorithm in use.

Author(s)

Danail Obreschkow

See Also

[griddata](#)

Examples

```
# make a mock sample of n d-dimensional points from
# three different components (1D line, 2D square, d-D normal distr)
d = 3 # number of dimensions of mock point set; try to choose different values 2, 3, 4, ...
n = 1e4 # number of particles per component
set.seed(1)
x = rbind(cbind(array(rep(runif(n,-1,1),2),c(n,2)),array(0,c(n,d-2))),
          cbind(array(runif(2*n),c(n,2)),array(0,c(n,d-2))),
          array(rnorm(d*n),c(n,d)))

# grid total projected probability density
npixels = 500 # number of pixels along a grid side
q = midseq(-3,3,npixels)
f1 = outer(dnorm(q),dnorm(q),'*')/3+outer(dunif(q),dunif(q),'*')/3
q = seq(round(npixels/3),round(npixels*2/3))
f1[q+npixels*(q-1)] = f1[q+npixels*(q-1)]+(npixels/6)^2/length(q)/3

# recover 2D projected pdf from 3D point sample using different methods
f2 = kde2(x, n=npixels, xlim=c(-3,3), ylim=c(-3,3), algorithm='basic', probability=TRUE)$field
f3 = kde2(x, n=npixels, xlim=c(-3,3), ylim=c(-3,3), algorithm='kdefast', probability=TRUE)$field
f4 = kde2(x, n=npixels, xlim=c(-3,3), ylim=c(-3,3), algorithm='kdenn', probability=TRUE)$field

# plot the 2D fields
img = function(f,x,y,title) {
  graphics::rasterImage(rasterflip(lim(f)^0.3),x,y,x+0.99,y+0.99)
  graphics::text(x+0.05,y+0.9,title,col='orange',pos=4)
}
oldpar = graphics::par(mar=rep(0.1,4))
nplot(c(0,2),c(0,2),asp=1)
img(f1,0,1,'Input pdf')
img(f2,1,1,'Random sample ("basic")')
img(f3,0,0,'Recovered pdf ("kdefast")')
img(f4,1,0,'Recovered pdf ("kdenn")')
graphics::par(oldpar)
```

landyszalay

Two-point correlation estimation

Description

Evaluates the Landy-Szalay (1993) estimator of the two-point correlation function of a point set D given a random comparison set R . The two point sets D and R can be made of different numbers of points, as the pair-counts are automatically normalized according to the number of points. In fact, it is often preferable to make the R set larger to reduce the R -related shot noise in the two-point estimator.

Usage

```
landyszalay(D, R, dr = 0.1, cpp = TRUE)
```

Arguments

D	n-element vector or n-by-d matrix of d-dimensional positions of the data points
R	m-element vector or m-by-d matrix of d-dimensional positions of the random comparison points
dr	bin size for the evaluation of the two-point correlation function
cpp	logical flag; if set to TRUE (default) a fast implementation in C++ is used to count the point-pairs in distance bins, otherwise the counting is performed less efficiently in R.

Value

Returns a data frame with the two-point statistics of the data points:

r	vector with the mid-points of the distance bins for which the two-point correlation function has been evaluated.
xi	values of the two-point correlation function at the distances r.
err	Poisson errors of xi.

Author(s)

Danail Obreschkow

See Also

[paircount](#)

last	<i>Last element of a vector</i>
------	---------------------------------

Description

Returns the last element of a vector or the n-th element counting from the end of a vector.

Usage

```
last(x, n = 1)
```

Arguments

x	vector
n	optional integer specifying the n-th element from the end to be returned

Value

scalar of the same type as x

Author(s)

Danail Obreschkow

lightness

Change lightness of a color

Description

Change lightness of a color

Usage

```
lightness(col, light = 0.5)
```

Arguments

col	is a color or vector/array of colors, specified as text (e.g. 'purple') or 7/9-character (e.g. '#A020F0')
light	lightness value, according to a HSL scheme, between 0 and 1 or a vector/array thereof

Value

Returns a 9-character color or vector/array of 9-character colors.

Author(s)

Danail Obreschkow

See Also

[transparent](#)

Examples

```
# Generate different lightnesses of the same color
plot(runif(50), runif(50), pch=20, cex=10, col=lightness('purple', runif(50)))
```

lim	<i>Crop values to a custom range</i>
-----	--------------------------------------

Description

Limits the values of a vector or array to a desired interval, while keeping the shape of the input argument

Usage

```
lim(x, min = 0, max = 1, clip = NULL, na = NULL)
```

Arguments

x	vector or array
min	minimum value
max	maximum value
clip	optional value specifying the value assigned to clipped data, e.g. clip=NA
na	optional value specifying the value assigned to non-numbers (NA and NaN)

Value

vector/array of the same shape as x

Author(s)

Danail Obreschkow

See Also

stretch

linfun	<i>Linear Function Fitter</i>
--------	-------------------------------

Description

Fits a global linear model $y = a + bx$ and returns a function that predicts y for arbitrary x , similar in spirit to [approxfun](#), but using a single least-squares line instead of piecewise interpolation.

Usage

```
linfun(x, y, na.rm = FALSE, ...)
```

Arguments

<code>x</code>	Numeric vector of predictor values.
<code>y</code>	Numeric vector of response values.
<code>na.rm</code>	Logical; if TRUE, remove NA, NaN, and infinite values before fitting (default: FALSE).
<code>...</code>	Additional arguments passed to lm .

Details

This is a convenience wrapper around [lm](#). It returns a callable function analogous to `approxfun`, but with a single global linear fit:

$$f(x) = a + bx,$$

where a and b are the intercept and slope from a least-squares regression of y on x .

Value

A function `f(xnew)` that evaluates the fitted linear regression at numeric values `xnew`.

See Also

`[stats::lm()], [stats::approxfun()]`

Examples

```
set.seed(1)
x = 1:10
y = 2 + 3 * x + rnorm(10)
f = linfun(x, y)
plot(x,y)
curve(f, col='red', add = TRUE) # show linear fit
points(6.6,f(6.6),col='red') # show predicted y-value at x = 6.6
```

linuxspaces

Handle spaces in Linux filenames

Description

Convert spaces in filenames (" ") to linux-type spaces "\ ", needed when calling `system()` on macOS.

Usage

```
linuxspaces(txt)
```

Arguments

`txt` filename, which may contain ordinary spaces, e.g. "my file 1.txt"

Value

filename with modified spaces, e.g. "my\ file\ 1.txt"

Author(s)

Danail Obreschkow

Examples

```
filename = '~/Desktop/my file 1.txt'
command = sprintf('ls -l %s',linuxspaces(filename))
## Not run:
system(command)

## End(Not run)
```

loadbin	<i>Read binary data into array</i>
---------	------------------------------------

Description

Reads binary data using the base function [readBin](#) and recasts it into an array of custom dimensions.

Usage

```
loadbin(
  filename,
  dim,
  bytes = 4,
  type = "numeric",
  signed = FALSE,
  endian = "little"
)
```

Arguments

filename	path of the file to be loaded
dim	vector specifying the dimensions of the array
bytes	number of bytes per number in the binary file
type	character vector of length describing the data type: "numeric" (default), "double", "integer", "int", "logical", "complex", "character", "raw"
signed	logical. Only used for integers of sizes 1 and 2, when it determines if the quantity on file should be regarded as a signed or unsigned integer.
endian	endian-type ("big" or "little") of the file

Value

Returns an array of dimension dim.

Author(s)

Danail Obreschkow

makeframe

Display a single movie frame

Description

Displays a single movie-frame in the R-console, exactly as used in a movie generated with [makemovie](#).

Usage

```
makeframe(
  frame.draw,
  frame.index,
  width = 1080,
  height = 720,
  cex = 1,
  oversampling = 1,
  pngfile = NULL
)
```

Arguments

frame.draw	function that plots an individual frame. This function must have exactly one argument 'x', which can be integer (e.g. a simple frame index) or real (e.g. a time).
frame.index	list of frame indices 'x' to be included in the movie
width	integer number of pixels along the horizontal axis
height	integer number of pixels along the vertical axis
cex	number defining the overall scaling of line widths, font sizes, etc.
oversampling	integer specifying the oversampling factor along both dimensions. If larger than 1, frames are plotted with (width*oversampling)-by-(height*oversampling) pixels and then resized back to width-by-height. This can be used to make line objects and text move more smoothly.
pngfile	optional path+filename of output file to save the image. R must have write access to this file.

Value

Returns the displayed image as n-by-m-by-4 array, representing the 4 RGBA channels of height n and width m.

Author(s)

Danail Obreschkow

See Also[makemovie](#)**Examples**

```
## Example: Movie of a manual clock

# Function to draw a single clock face with two hands
frame = function(time) {
  oldpar = graphics::par(mar=c(0,0,0,0))
  nplot(xlim=c(-1.1,1.1),ylim=c(-1.1,1.1),pty='s')
  plotrix::draw.circle(0,0,1,col='#aaaaff')
  radius = c(0.5,0.9)
  speed = 2*pi/c(720,60)
  lwd = c(4,2)
  graphics::arrows(0,0,radius*sin(speed*time),radius*cos(speed*time),lwd=lwd)
  graphics::par(oldpar)
}

# Produce movie
## Not run:
makeframe(frame,15,200,200)

## End(Not run)
```

makemovie

*Produce a movie from frame-drawing function***Description**

Generates an MP4-movie provided a custom function that plots individual frames. The routine has been developed and tested for MacOS and it requires on a working installation of ffmpeg.

Usage

```
makemovie(
  frame.draw,
  frame.index,
  output.path,
  output.filename,
  width = 1080,
  height = 720,
  fps = 60,
```

```

    keep.frames = FALSE,
    quiet = FALSE,
    separator = "/",
    ffmpeg.cmd = "ffmpeg",
    ffmpeg.opt = "-vcodec libx264 -crf 18 -pix_fmt yuv420p",
    manual = FALSE,
    cex = 1,
    oversampling = 1,
    first.index = 1,
    last.index = length(frame.index)
  )

```

Arguments

<code>frame.draw</code>	function that plots an individual frame. This function must have exactly one argument 'x', which can be integer (e.g. a simple frame index) or real (e.g. a time).
<code>frame.index</code>	list of frame indices 'x' to be included in the movie
<code>output.path</code>	character specifying the directory, where the movie and temporary frames are saved
<code>output.filename</code>	movie filename without path. This filename should end on the extension '.mp4'.
<code>width</code>	integer number of pixels along the horizontal axis
<code>height</code>	integer number of pixels along the vertical axis
<code>fps</code>	number of frames per second
<code>keep.frames</code>	logical flag specifying whether the temporary directory with the individual frame files should be kept. If <code>manual</code> is set to <code>TRUE</code> , the frames are always kept.
<code>quiet</code>	logical flag; if true, all console outputs produced by 'ffmpeg' are suppressed
<code>separator</code>	filename separate of the system ('/' for Mac, Linux, Unix; '\\' for Windows)
<code>ffmpeg.cmd</code>	command used to call ffmpeg from a terminal. Normally, this is just 'ffmpeg'.
<code>ffmpeg.opt</code>	compression and formatting options used with ffmpeg
<code>manual</code>	logical flag; if true, ffmpeg is not called from within the code and the frames are never deleted. The suggested linux command line is returned as output.
<code>cex</code>	number defining the overall scaling of line widths, font sizes, etc.
<code>oversampling</code>	integer specifying the oversampling factor along both dimensions. If larger than 1, frames are plotted with (width*oversampling)-by-(height*oversampling) pixels and then resized back to width-by-height. This can be used to make line objects and text move more smoothly.
<code>first.index</code>	integer specifying the first index of the vector <code>frame.index</code> to consider. Choosing a value larger than the default (1) can be used to continue a previously interrupted call of <code>makemovie</code> and/or to call <code>makemovie</code> from different R sessions in parallel.
<code>last.index</code>	integer specifying the last index of the vector <code>frame.index</code> to consider. Choosing a value smaller than the default (<code>length(frame.index)</code>) can be used to continue a previously interrupted call of <code>makemovie</code> and/or to call <code>makemovie</code> from different R sessions in parallel.

Value

Linux command line to convert frames into movie using ffmpeg.

Author(s)

Danail Obreschkow

See Also

[makeframe](#)

Examples

```
## Example: Movie of a manual clock

# Function to draw a single clock face with two hands
frame = function(time) {
  oldpar = graphics::par(mar=c(0,0,0,0))
  nplot(xlim=c(-1.1,1.1),ylim=c(-1.1,1.1),pty='s')
  plotrix::draw.circle(0,0,1,col='#aaaaff')
  radius = c(0.5,0.9)
  speed = 2*pi/c(720,60)
  lwd = c(4,2)
  graphics::arrows(0,0,radius*sin(speed*time),radius*cos(speed*time),lwd=lwd)
  graphics::par(oldpar)
}

# Produce movie
## Not run:
makemovie(frame,seq(0,60,0.5),'~/testmovie','movie.mp4',200,200)

## End(Not run)
```

Description

Numerical integration using a Monte Carlo (MC) or Quasi-Monte Carlo (QMC) algorithm, based on a Halton sequence. These algorithms are of low order ($1/\sqrt{n}$ for MC, $\log(n)/n$ for QMC in one dimension) compared to the typical orders of 1D deterministic integrators, such as those available in the `integrate` function. The MC and QMC integrators are suitable to compute D-dimensional integrals with $D \gg 1$, since the order of most deterministic methods deteriorates exponentially with D, whereas the order of MC remains $1/\sqrt{n}$, irrespective of D, and the order of QMC only deteriorates slowly with D as $\log(n)^D/n$.

Usage

```
mcintegral(f, a, b, n = 1e+05, qmc = FALSE, seed = NULL, warn = TRUE)
```

Arguments

f	scalar function of a D-vector to be integrated numerically; for fast performance, this function should be vectorized, such that it returns an N-element vector if it is given an N-by-D matrix as argument. An automatic warning is produced if the function is not vectorized in this manner.
a	D-vector with lower limit(s) of the integration
b	D-vector with upper limit(s) of the integration
n	approximate number of random evaluations. (The exact number is $\max(1, \text{round}(\sqrt{n}))^2$.)
qmc	logical flag. If false (default), pseudo-random numbers are used; if true, quasi-random numbers from a D-dimensional Halton sequence are used.
seed	optional seed for random number generator. Only used if qmc is false.
warn	logical flag. If true (default), a warning is produced if the function f is not vectorized.

Value

Returns a list of items:

value	the best estimate of the integral.
error	an estimate of the statistical 1-sigma uncertainty.
iterations	exact number of evaluations (close to n).

Author(s)

Danail Obreschkow

Examples

```
## Numerically integrate sin(x)
f = function(x) sin(x)
m = mcintegral(f,0,pi)
cat(sprintf('Integral = %.3f\u00B1%.3f (true value = 2)\n',m$value,m$sigma))

## Numerically compute the volume of a unit sphere
sphere = function(x) as.numeric(rowSums(x^2)<=1) # this is vectorized
vmc = mcintegral(sphere,rep(-1,3),rep(1,3),seed=1)
vqmc = mcintegral(sphere,rep(-1,3),rep(1,3),qmc=TRUE)
cat(sprintf('Volume of unit sphere = %.3f\u00B1%.3f (MC)\n',vmc$value,vmc$error))
cat(sprintf('Volume of unit sphere = %.3f\u00B1%.3f (QMC)\n',vqmc$value,vqmc$error))
cat(sprintf('Volume of unit sphere = %.3f (exact)\n',4*pi/3))
```

midseq	<i>Mid-points of regular grid</i>
--------	-----------------------------------

Description

Compute the mid-point positions of a one-dimensional regular grid of n equal intervals.

Usage

```
midseq(min, max, n = 1)
```

Arguments

min	left boundary of first bin
max	right boundary of last bin
n	number of bins

Value

vector of mid points

Author(s)

Danail Obreschkow

mollweide	<i>Mollweide projection</i>
-----------	-----------------------------

Description

Performs a Mollweide projection (also known as Babinet projection, homolographic projection, homolographic projection, and elliptical projection) of longitude and latitude coordinates. The most important feature of the Mollweide projection is that it preserves surface areas, which makes it a commonly used projection in geography, astronomy and cosmology. The total surface area of the standard projection is equal to the surface area of the unit sphere (4π); and the shape of the fully projected sphere is an ellipse (with axes lengths $2\sqrt{2}$ and $\sqrt{2}$).

Usage

```
mollweide(lon, lat, lon0 = 0, radius = 1, deg = FALSE)
```

Arguments

lon	n-vector of longitudes in radian (unless deg=TRUE)
lat	n-vector of latitudes in radian (unless deg=TRUE), must lie between -pi/2 and +pi/2
lon0	latitude of null meridian, which will be projected on to x=0
radius	radius of spherical projection, such that the surface area of the projection equals 4*pi*radius^2
deg	logical flag; if set to TRUE, the input arguments lon, lat, lon0 are assumed to be in degrees (otherwise in radians)

Value

Returns an n-by-2 matrix of 2D Cartesian coordinates x and y.

Author(s)

Danail Obreschkow

Examples

```
lon = runif(1e4,0,2*pi)
lat = asin(runif(1e4,-1,1)) # = uniform sampling of the sphere
plot(mollweide(lon,lat),xlim=c(-3,3),ylim=c(-1.5,1.5),pch=16,cex=0.5)
plotrix::draw.ellipse(0,0,2*sqrt(2),sqrt(2),border='orange',lwd=2)
```

moments	<i>Second moment tensor</i>
---------	-----------------------------

Description

Computes the second moment tensor of a set of point masses in arbitrary dimensions,

$$\mathbf{M} = \sum_i m_i \mathbf{x}_i \mathbf{x}_i^T.$$

Usage

```
moments(x, m = 1)
```

Arguments

x	Numeric vector or matrix. If a matrix is supplied, each row is interpreted as a point.
m	Numeric scalar or vector of point masses. If a scalar is supplied, the same mass is assigned to every point.

Value

A symmetric $d \times d$ matrix containing the second moment tensor, where d is the dimension of the points.

See Also

[quadrupole](#), [inertia](#)

mutual	<i>Mutual information of two random variables</i>
--------	---

Description

Computes the mutual information of two random variables X and Y, given their 2D density represented in a matrix.

Usage

```
mutual(x, y = NULL, b = exp(1), n = NULL, xlim = NULL, ylim = NULL)
```

Arguments

x	either of the following: (1) an m-by-n matrix representing the 2D probability mass function of two random variables X and Y; all elements must be non-negative; the normalization is irrelevant. (2) an n-vector of sampled x-values; in this case y must be specified.
y	optional vector of sampled y-values (only used if x is a vector of x-values).
b	base of the logarithm in mutual information $I(X,Y)$. Default is e.
n	scalar or 2-element vector specifying the number of equally space grid cells. Only used if x and y are vectors. If not provided, the default is $n=0.2*\sqrt{\text{length}(x)}$, bound between 2 and 1000. Note that $n \sim \sqrt{\text{length}(x)}$ keeps the mutual information constant for random data sets of different size.
xlim	2-element vector specifying the x-range (data cropped if necessary). Only used if x and y are vectors. If not given, xlim is set to the range of x.
ylim	2-element vector specifying the y-range (data cropped if necessary). Only used if x and y are vectors. If not given, ylim is set to the range of y.

Value

Returns a list of items:

I	standard mutual information $I(X,Y)$.
N	normalized mutual information $I(X,Y)/\sqrt{H(X)*H(Y)}$, where H is the Shannon information entropy.

Author(s)

Danail Obreschkow

ndft

*Non-uniform Discrete Fourier Transform***Description**

Compute the one-dimensional Non-uniform Discrete Fourier Transform (NDFT). This is needed if the data are sampled at irregularly spaced times.

Usage

```
ndft(
  f,
  x = seq(0, length(f) - 1)/length(f),
  nu = seq(0, length(f) - 1),
  inverse = FALSE,
  weighing = TRUE,
  simplify = TRUE
)
```

Arguments

<code>f</code>	vector of real or complex function values
<code>x</code>	vector of points in direct space, typically time or position coordinates. If <code>inverse=FALSE</code> , <code>x</code> must have the same length as <code>f</code> .
<code>nu</code>	vector of frequencies in units of $[1/\text{units of } x]$. If <code>inverse=TRUE</code> , <code>nu</code> must have the same length as <code>f</code> .
<code>inverse</code>	logical flag; if <code>TRUE</code> , the inverse Fourier transform is performed.
<code>weighing</code>	logical flag; if <code>TRUE</code> , irregularly spaced evaluations of <code>f</code> will be weighted proportionally to their bin width in <code>x</code> (if <code>inverse=FALSE</code>) or <code>nu</code> (if <code>inverse=FALSE</code>).
<code>simplify</code>	logical flag; if <code>TRUE</code> , the complex output array will be simplified to a real array, if it is real within the floating point accuracy.

Details

The one-dimensional NDFT of a vector $f = (f_1, \dots, f_N)$ is defined as

$$F_j = \sum_i w_i f_i \exp(-2\pi i * x_i * \nu_j)$$

where w_i are optional weights, proportional to the interval around x_i , only used if `weighing=TRUE`. Likewise, the inverse NDFT is defined as

$$f_i = \sum_j w_j F_j \exp(+2\pi i * x_i * \nu_j)$$

where w_j are optional weights, proportional to the interval around ν_j . In this implementation NDFTs are computed using a brute force algorithm, scaling as $O(N * N)$, which is considerably worse than the $O(N) * \log(N)$ scaling of FFT algorithms. It is therefore important to pick the required frequencies wisely to minimise computing times.

Value

Returns a vector of the same length as `x` (if `inverse=FALSE`) or `nu` (if `inverse=TRUE`).

Author(s)

Danail Obreschkow

See Also

[fft](#)

Examples

```
# Define an example signal
nu1 = 1 # [Hz] first frequency
nu2 = 8 # [Hz] second frequency in the signal
s = function(t) sin(2*pi*nu1*t)+0.7*cos(2*pi*nu2*t+5)

# Discretize signal
N = 50 # number of samples
t.uniform = seq(0,N-1)/N
t.nonuniform = t.uniform^1.3
s.uniform = s(t.uniform)
s.nonuniform = s(t.nonuniform)

# Plot signal
oldpar = par(mfrow = c(1, 2))
curve(s,0,1,500,xaxs='i',main='Time signal',xlab='Time t',ylab='s(t)',col='grey')
points(t.uniform,s.uniform,pch=16,cex=0.8)
points(t.nonuniform,s.nonuniform,pch=4,col='blue')
legend('topright',c('Continuous signal','Uniform sample','Non-uniform sample'),
      lwd=c(1,NA,NA),pch=c(NA,16,4),col=c('grey','black','blue'),pt.cex=c(1,0.8,1))

# Uniform and non-uniform DFT
nu = seq(0,N-1) # discrete frequencies
spectrum.uniform = stats::fft(s.uniform)
spectrum.nonuniform = ndft(s.nonuniform,t.nonuniform,nu)
spectrum.wrong = stats::fft(s.nonuniform)

# Evaluate power
power.uniform = Mod(spectrum.uniform)^2
power.nonuniform = Mod(spectrum.nonuniform)^2
power.wrong = Mod(spectrum.wrong)^2

# Plot DFT and NDFT up to Nyquist frequency
plot(nu,power.uniform,pch=16,cex=0.8,xlim=c(0,N/2),xaxs='i',
     main='Power spectrum',xlab=expression('Frequency'~nu~'[Hz]'),ylab='Power')
points(nu,power.nonuniform,pch=4,col='blue')
points(nu,power.wrong,pch=1,col='red')
abline(v=c(nu1,nu2),col='grey',lty=2)
legend('topright',c('DFT of uniform sample','NDFT of non-uniform sample',
  'DFT of non-uniform sample (wrong)','Input frequencies'),
```

```
lwd=c(NA,NA,NA,1),lty=c(NA,NA,NA,2),pch=c(16,4,1,NA),
col=c('black','blue','red','grey'),pt.cex=c(0.8,1,1,NA))
par(oldpar)
```

ngon

Draw a regular n-gon

Description

Draws a regular polygon with n sides, such as a triangle (n=3) or hexagon (n=6).

Usage

```
ngon(x = 0, y = 0, s = 1, n = 6, angle = 0, fix.aspect = TRUE, ...)
```

Arguments

x	vector of x-coordinates specifying the centres of the n-gons.
y	vector of y-coordinates specifying the centres of the n-gons.
s	side lengths; either a single number or a vector of the same length as x and y. In log-log plots, the value of s is in units of dex.
n	number of sides of the regular n-gons; either a single number or a vector of the same length as x and y.
angle	rotation angle in radians; either a single number or a vector of the same length as x and y.
fix.aspect	logical flag. If TRUE (default), the aspect ratio of the n-gon on the screen is forced to be unity, even if this makes it irregular in the coordinates of the plot. If FALSE, the n-gon is regular in plot coordinates, which makes it distorted in screen coordinates if the aspect ratio is not one and/or if logarithmic coordinates are used.
...	additional arguments used by polygon .

Value

None.

Author(s)

Danail Obreschkow

Examples

```
## Plot random points on the unit sphere in Mollweide projection
# hexagon at the center of a plot
nplot(bty='o', asp=0.5)
ngon(x=0.5, y=0.5, s=0.1, n=6, fix.aspect=FALSE)

ngon(x=0.5, y=0.5, s=0.1, n=6, border='red')

plot(NA,xlim=c(1,1e3),ylim=c(1,1e5),log='xy')
ngon(x=10^runif(10,0,3), y=10^runif(10,0,5), s=1, n=6, border='red',lwd=3)
```

nplot	<i>Make empty plot area</i>
-------	-----------------------------

Description

Open an empty plot

Usage

```
nplot(
  xlim = c(0, 1),
  ylim = c(0, 1),
  xlab = "",
  ylab = "",
  xaxs = "i",
  yaxs = "i",
  xaxt = "n",
  yaxt = "n",
  bty = "n",
  ...
)
```

Arguments

xlim, ylim	vectors with plotting limits.
xlab, ylab	horizontal and vertical labels.
xaxs, yaxs	style of the axis interval (see par).
xaxt, yaxt	character which specifies the x axis type (see par).
bty	character specifying the border type (see par).
...	additional arguments used by plot

Value

None

Author(s)

Danail Obreschkow

paircount*Count the number of point-pairs in distance bins*

Description

Count the number of point-pairs in equally spaced distances bins. Code works in any dimension. If only one point set is provided, the distances of this point set with itself are used (counting each pairs only once, i.e. only ij, not ji).

Usage

```
paircount(x, y = NULL, dr, rmax, cpp = TRUE)
```

Arguments

x	n-element vector or n-by-d matrix of d-dimensional positions of data points
y	optional m-element vector or m-by-d matrix of d-dimensional positions of a second point set
dr	distance bin size
rmax	maximum distance to be considered
cpp	logical flag; if set to TRUE (default) a fast implementation in C++ is used, otherwise the counting is performed less efficiently in R.

Value

Returns a data frame of two column vectors:

r	mid-points of the distance bins.
n	number of pairs in the distance bin.

Author(s)

Danail Obreschkow

See Also[landyszalay](#)

`pdf2jpg`*Convert pdf to jpg*

Description

Calls the console "convert" function to convert a pdf-file into a jpeg-image. Requires "convert" to be installed already.

Usage

```
pdf2jpg(  
  pdf.filename,  
  jpg.filename,  
  quality = 100,  
  background = "white",  
  dim = c(1600, 1200),  
  remove.pdf = FALSE,  
  verbose = TRUE  
)
```

Arguments

<code>pdf.filename</code>	filename of pdf input file
<code>jpg.filename</code>	filename of jpeg output file
<code>quality</code>	quality of jpeg compression from 1 (worst) to 100 (best)
<code>background</code>	color of background
<code>dim</code>	size in pixels of the jpeg-image
<code>remove.pdf</code>	logical flag. If TRUE, the pdf file is deleted after the conversion.
<code>verbose</code>	logical flag to turn on/off console statements.

Value

None

Author(s)

Danail Obreschkow

planckcolors	<i>Planck CMB colour palette</i>
--------------	----------------------------------

Description

Generates a colour scale that closely mimics the official colours used to display the Planck CMB temperature map from -300uK to +300uK.

Usage

```
planckcolors(n)
```

Arguments

n	integer number of colors in the scale
---	---------------------------------------

Value

Returns an n-vector of RGB colour strings.

Author(s)

Danail Obreschkow

Examples

```
nplot()
rasterImage(rbind(planckcolors(1e3)),0,0,1,1)
```

pol2car	<i>Polar/cylindrical to Cartesian coordinate conversion</i>
---------	---

Description

Convert polar/cylindrical coordinates to 2D/3D Cartesian coordinates

Usage

```
pol2car(x)
```

Arguments

x	2/3-element or n-by-2/3 matrix representing the polar/cylindrical coordinates (r,phi)/(r,phi,z), where phi=0...2*pi is the azimuth measured positively from the x-axis.
---	---

Value

Returns a 2/3-element vector or a n-by-2/3 element matrix representing the Cartesian coordinates (x,y)/(x,y,z).

Author(s)

Danail Obreschkow

See Also

[car2pol](#)

progress

Show progress while timer is running

Description

Show progress while a timer is running following a call of tick(). To suppress all progress updates, set the environment variable .cooltools.env\$suppressProgress to TRUE.

Usage

```
progress(txt = NULL)
```

Arguments

txt	custom text to be displayed. If not provided, the time since calling tick() is displayed.
-----	---

Value

None

Author(s)

Danail Obreschkow

See Also

[tick tock error](#)

Examples

```

tick('Test')
Sys.sleep(.1)
for (i in seq(3)) {
  progress(i)
  Sys.sleep(.1)
}
tock()

```

quadrupole

Quadrupole tensor

Description

Computes the trace-free mass quadrupole tensor of a set of point masses in arbitrary dimensions,

$$\mathbf{Q} = \sum_i m_i (d \mathbf{x}_i \mathbf{x}_i^T - |\mathbf{x}_i|^2 \mathbf{I}) ,$$

where d is the dimensionality of the points and $\mathbf{I}$ is the $d \times d$ identity matrix.

Usage

```
quadrupole(x, m = 1)
```

Arguments

<code>x</code>	Numeric vector or matrix. If a matrix is supplied, each row is interpreted as a point.
<code>m</code>	Numeric scalar or vector of point masses. If a scalar is supplied, the same mass is assigned to every point.

Value

A symmetric $d \times d$ matrix containing the trace-free quadrupole tensor.

See Also

[moments](#), [inertia](#)

quiet	<i>Suppress console output</i>
-------	--------------------------------

Description

Executes routines and command lines and load packages while suppressing the console output.

Usage

```
quiet(x)
```

Arguments

x routine to be called

Value

Returns whatever the called routine returns in invisible form.

Author(s)

Danail Obreschkow

Examples

```
# Test function
test = function(x) {
  cat('This routine is likes to talk a lot!\n')
  return(x^2)
}

# Standard call call:
y = test(5)
print(y)

# Quiet call:
y = quiet(test(6))
print(y)
```

rasterflip	<i>Flip array to be displayed with rasterImage()</i>
------------	--

Description

Flips the array A to be displayed with rasterImage, such that the first index runs from left to right and second index runs from bottom to top, like in standard Cartesian coordinates. In this way rasterImage(rasterflip(A)) has the same orientation as image(A).

Usage

```
rasterflip(A)
```

Arguments

A	n-by-m array of a monochromatic image or n-by-m-by-k array of a color image (where k is 3 or 4)
---	---

Value

A m-by-n array of a monochromatic image or m-by-n-by-k array of a color image.

Author(s)

Danail Obreschkow

readhdf5	<i>Read data from an HDF5 file</i>
----------	------------------------------------

Description

Reads data from an HDF5 file, including attributes, into a nested list that preserves the hierarchical structure of the HDF5 data. The routine can read 64-bit integers and represent them as 64-bit integers in R via the bit64 package. It can also read 32-bit floating-points values, not part of native R. These are automatically converted into 64-bit doubles.

Usage

```
readhdf5(file, subtree = "*", group.attr.as.data = FALSE, empty = FALSE)
```

Arguments

file	Character string specifying the file name of the input HDF5 file.
subtree	A structure specifying the HDF5 groups and datasets to be read. Use an asterisk "*" (default) to read the entire file. To read only part of the file, provide a named list reflecting the hierarchy of groups, subgroups, and datasets. For (sub)groups, use nested lists containing the items to read, or use '*' to load everything in the group. An empty list list() reads only the attributes of a group. For datasets, use NULL to read only attributes, or any other content to read the full data.
group.attr.as.data	Logical flag. If TRUE, group attributes are converted to datasets, which is useful for formats where parameters are stored as attributes (e.g., Gadget simulation outputs).
empty	Logical flag. If TRUE, only names of groups and datasets are returned, with all data equal to NA. This is a fast way of reading the hierarchical structure.

Details

This function, based on the hdf5r package, recursively parses and reads HDF5 files into nested lists that preserve the original hierarchy. Attributes in groups and datasets are included in the output.

Value

Nested list representing the contents of the HDF5 file. Groups are nested sublists, datasets are represented by their data. Attributes of groups and datasets are attached as attributes to the corresponding sublists and data elements.

See Also

[writehdf5](#) for examples.

rebindensity	<i>Re-bin density histograms</i>
--------------	----------------------------------

Description

Transform density histogram data into histogram data with different bins

Usage

```
rebindensity(x, y, xout)
```

Arguments

x	n-vector giving the mid-points of the input histogram bins, must be equally spaced
y	n-vector giving the values of the input histogram values
xout	m-vector giving the mid-points of the output histogram bins, must be equally spaced

Value

m-vector of y-values associated with the bins specified by xout.

Author(s)

Danail Obreschkow

Examples

```
# original binning
x = seq(0.5,4.5)
y = seq(5)
plot(x,y,xlim=c(-1,6),ylim=c(0,6),pch=16)
lines(histcoord(x,y),lwd=3)

# rebinning
xout = seq(-0.9,6,0.3)
yout = rebindensity(x,y,xout)
points(xout,yout,col='red',pch=16)
lines(histcoord(xout,yout),col='red')
```

 rng

Random number generator for a custom d-dimensional distribution

Description

Brute-force algorithm for drawing random numbers from a d-dimensional distribution.

Usage

```
rng(f, n, min, max, fmax = NULL, quasi = FALSE, start = 1, warn = TRUE)
```

Arguments

f	function of a d-vector representing a d-dimensional distribution function. This function must be non-negative on the whole domain. It does not need to be normalized. For fast performance, this function should be vectorized, such that it returns an N-element vector if it is given an N-by-D matrix as argument. An automatic warning is produced if the function is not vectorized in this manner.
n	number of random numbers to be generated
min, max	are d-vectors specifying the domain of distribution function; the domain must be finite and should be as restrictive as possible to keep the number of random trials as low as possible.
fmax	maximum value of f on its domain. If set to NULL (default), this value will be determined automatically, using the optimize (if d=1) and optim (if d>1) function with its default options. A value for fmax should be set, if the automatically determined value (see output list) is incorrect.

quasi	logical flag. If true, quasi-random numbers with low-discrepancy are drawn, based on a Halton sequence. Otherwise, the standard internal pseudo-random generator of <code>runif()</code> is used.
start	starting index of Halton sequence. Only used if <code>quasi=TRUE</code> .
warn	logical flag. If true, a warning is produced if the function <code>f</code> is not vectorized.

Value

Returns list of items:

x	n-by-d matrix of n random d-vectors.
fmax	maximum value of the distribution function <code>f</code> on the domain.
n	number of random vectors (same as argument <code>n</code>).
ntrials	number of trials.

Author(s)

Danail Obreschkow

See Also

[dpqr](#)

Examples

```
## 1D random number generation from a sine-function
f = function(x) sin(x)
out.pseudo = rng(f,1e3,0,pi)
out.quasi = rng(f,1e3,0,pi,quasi=TRUE)
hist(out.pseudo$x,100,freq=FALSE,border=NA,xlab='x',main='sine-distribution')
hist(out.quasi$x,100,freq=FALSE,border=NA,col='#ff000066',add=TRUE)
curve(sin(x)/2,0,pi,add=TRUE)

## 2D quasi-random sampling of a disk with exponentially declining surface density
f = function(x) exp(-sqrt(x[,1]^2+x[,2]^2))
out = rng(f,1e4,min=c(-5,-5),max=c(5,5),quasi=TRUE)
plot(out$x,cex=0.3,pch=16,asp=1,main='Quasi-random exponential disk')

## 5D random number generation (5-dimensional sphere)
f = function(x) as.numeric(sum(x^2)<=1)
out = rng(f,1e4,rep(-1,5),rep(1,5))
cat(sprintf('Number of successes over number of trials : %.4f\n',out$n/out$ntrials))
cat(sprintf('Expected ratio for n=\u221E : %.4f\n',pi^(5/2)/gamma(1+5/2)/2^5))
```

rotation2	<i>2D rotation matrix</i>
-----------	---------------------------

Description

Compute a 2D rotation matrix given a rotation angle

Usage

```
rotation2(angle)
```

Arguments

angle	rotation angle in radians (counter-clockwise)
-------	---

Value

Returns a 2-by-2 anti-symmetric rotation matrix

Author(s)

Danail Obreschkow

See Also

[rotation3](#)

rotation3	<i>3D rotation matrix</i>
-----------	---------------------------

Description

Compute a 3D rotation matrix given an axis and an angle

Usage

```
rotation3(u, angle = NULL)
```

Arguments

u	3-vector specifying the rotation axis
angle	rotation angle in radians; if not given, the norm of the vector u is interpreted as the angle

Value

Returns a 3-by-3 rotation matrix

Author(s)

Danail Obreschkow

See Also[rotation2](#)

runif2

*Generate randomly oriented vectors in 2D***Description**

Generate randomly oriented vectors in 2D, following an isotropic distribution (optionally truncated to a region).

Usage

```
runif2(n = 1, r = c(0, 1), azimuth = c(0, 2 * pi), quasi = FALSE, start = 1)
```

Arguments

n	number of random vectors to be generated
r	2-vector specifying the range of radii
azimuth	2-vector specifying the range of azimuth angles
quasi	logical flag. If true, quasi-random numbers with low-discrepancy are drawn, based on a Halton sequence. Otherwise, the standard internal pseudo-random generator of <code>runif()</code> is used.
start	starting index of Halton sequence. Only used if <code>quasi=TRUE</code> .

Value

Returns an n-by-2 array of n vectors.

Author(s)

Danail Obreschkow

See Also[runif3](#)**Examples**

```
## generate 500 unit vectors with radii between 0.5 and 1
x = runif2(500,r=c(0.5,1))
oldpar = par(pty='s')
plot(x,pch=20)
par(oldpar)
```

runif3

*Generate randomly oriented vectors in 3D***Description**

Generate randomly oriented vectors in 3D, following an isotropic distribution (optionally truncated to a region).

Usage

```
runif3(
  n = 1,
  r = c(0, 1),
  azimuth = c(0, 2 * pi),
  polarangle = c(0, pi),
  quasi = FALSE,
  start = 1
)
```

Arguments

n	number of random vectors to be generated
r	2-vector specifying the range of radii
azimuth	2-vector specifying the range of azimuth angles (maximum range 0..2*pi)
polarangle	2-vector specifying the range of polar angles (maximum range 0..pi)
quasi	logical flag. If true, quasi-random numbers with low-discrepancy are drawn, based on a Halton sequence. Otherwise, the standard internal pseudo-random generator of runif() is used.
start	starting index of Halton sequence. Only used if quasi=TRUE.

Value

Returns an n-by-3 array of n vectors.

Author(s)

Danail Obreschkow

See Also

[runif2](#)

Examples

```
## draw 20 unit vectors on a sphere
x = runif3(20,r=c(1,1))
print(rowSums(x^2))
```

scalarproduct	<i>Scalar product</i>
---------------	-----------------------

Description

Computes the scalar (dot) product of vectors. The inputs may be individual vectors or matrices whose rows represent vectors.

Usage

```
scalarproduct(x, y)
```

Arguments

x, y	Numeric vectors or matrices. If a matrix is supplied, each row is interpreted as a vector.
------	--

Value

Returns either a scalar (vector-vector case) or a vector containing the row-wise scalar products.

See Also

[scalarproduct](#), [vectornorm](#), [unitvector](#)

sigmoid	<i>Sigmoid function</i>
---------	-------------------------

Description

Returns S-shaped functions, monotonically increasing between two constants with a point symmetry at the half-way point.

Usage

```
sigmoid(x, type = 1, fmin = 0, fmax = 1, xmid = 0, slope = 1)
```

Arguments

x	real argument between -Inf and +Inf, can be a vector
type	number or character string, specifying the type of function. The following expressions vary between -1 and +1 with a slope of 1 at the symmetry x=0. tanh (1): hyperbolic tangent function, $\tanh(x)$, which becomes the logistic function, $1/(1+\exp(-x))$, if all arguments kept at default. atan (2): arctangent function, $2/\pi \cdot \text{atan}(\pi/2 \cdot x)$ err (3): error function, $\text{erf}(\sqrt{\pi}/2 \cdot x)$

sqrt (4): algebraic function with root, $x/\sqrt{1+x^2}$
 abs (5): algebraic function with absolute value, $x/(1+\text{abs}(x))$
 gd (6): Gudermannian function, $4/\pi \cdot \text{atan}(\tanh(\pi/4 \cdot x))$

fmin asymptotic function minimum at $x=-\text{Inf}$
 fmax asymptotic function maximum at $x=+\text{Inf}$
 xmid point of symmetry, where the function value is $(\text{fmin}+\text{fmax})/2$
 slope slope of the function at $x=\text{xmid}$

Value

Returns a vector with the same number of elements as x

Author(s)

Danail Obreschkow

Examples

```
col = c('red','orange','#cccc00','#00bb00','blue','purple')
for (i in seq(6)) {
  graphics::curve(sigmoid(x,i),-3,3,add=i>1,col=col[i],ylab='sigmoid(x)')
}
graphics::lines(c(-1.5,1.5),c(-1,2),lty=2)
```

smartround

Round a vector of floating-point values while preserving their sum

Description

Rounds the values in a vector up and down, preserving the sum of the vector and minimizing the total rounding error under this condition. An example where this is useful is when rounding a vector of percentages, where the total should add up to 100 percent.

Usage

```
smartround(x, digits = 0)
```

Arguments

x vector of values
 digits optional non-negative integer specifying the number of digits of the rounded numbers

Value

Returns a vector of rounded values of the same length as x .

Author(s)

Danail Obreschkow

Examples

```
x = runif(5)
x = x/sum(x)*100
print(x)
print(sum(x))
y = smartround(x)
print(y)
print(sum(y))
y2 = smartround(x,2)
print(y2)
print(sum(y2))
```

smoothcontour

*Draw smoothed contours***Description**

Draw smoothed iso-countours for a density field. The contours are computed using the [contourLines](#) routine and smoothed using the [smooth.spline](#) function. Both open and closed contour lines are handled correctly.

Usage

```
smoothcontour(
  x = seq(0, 1, length.out = nrow(z)),
  y = seq(0, 1, length.out = ncol(z)),
  z,
  levels,
  smoothing = 0.5,
  min.radius = 1,
  lwd = 1,
  lty = 1,
  col = "black",
  ...
)
```

Arguments

x, y	vectors containing the locations of grid lines at which the values of z are measured. These must be in ascending order. By default, equally spaced values from 0 to 1 are used.
z	matrix representing the density field on which the contours are plotted.

levels	vector of the iso-contour levels.
smoothing	value between 0 and 1 specifying the degree of smoothing.
min.radius	numerical value. If larger than 0, all contours with a mean radius (in pixels) below min.radius are removed.
lwd	vector of line widths (see par)
lty	vector of line types (see par)
col	vector of colors (see par)
...	additional parameters to be passed to the function lines .

Value

None

Author(s)

Danail Obreschkow

See Also[contourLines](#), [smooth.spline](#)**Examples**

```

set.seed(1)
f = function(x) cos(2*x[1]-x[2]-1)^2*exp(-x[1]^2-x[2]^2-x[1]*x[2])
x = seq(-3,3,length=100)
m = pracma::meshgrid(x)
z = array(Vectorize(function(x,y) f(c(x,y)))(m$Y,m$X)+rnorm(4e4,sd=0.1),dim(m$X))
image(x,x,z,col=terrain.colors(100))
contour(x,x,z,levels=c(0.2,0.5),add=TRUE)
smoothcontour(x,x,z,levels=c(0.2,0.5),lwd=3,smoothing=0.8,min.radius=2)

```

smoothfun

*Smoothed Function***Description**

Generates a cubic smoothed spline function $y=f(x)$ approximating supplied (x,y)-data with a custom number of degrees of freedom. The routines builds on [smooth.spline](#), but directly returns the smoothed function rather than the fitted model.

Usage

```
smoothfun(x, y = NULL, w = NULL, df = NULL, ...)
```

Arguments

x	a vector giving the values of the predictor variable, or a list or a two-column matrix specifying x and y.
y	responses. If y is missing or NULL, the responses are assumed to be specified by x, with x the index vector.
w	optional vector of weights of the same length as x; defaults to all 1.
df	the desired equivalent number of degrees of freedom. Must be in [2,nx], where nx is the number of unique x values. If not given, nx is set to the square root of the number of unique x-values.
...	additional optional arguments used by smooth.spline .

Value

Returns a fast and vectorized smoothed function $f(x)$.

Author(s)

Danail Obreschkow

See Also

[smooth.spline](#)

Examples

```
# make random data set
set.seed(1)
x = runif(100)
y = sin(2*pi*x)+rnorm(100, sd=0.5)
plot(x,y,pch=16)

# smoothed spline
f = smoothfun(x, y)
curve(f, add=TRUE, col='red')

# smoothed spline with custom degree of freedom
g = smoothfun(x, y, df=5)
curve(g, add=TRUE, col='blue')
```

sortlist

Sort List Entries Alphabetically

Description

This function sorts the entries of a structured list in alphabetical order, including all nested sublists recursively, making it easier to navigate nested list structures and compare different lists. Un-named items are listed last. Attributes of the original list are preserved.

Usage

```
sortlist(lst, recursive = TRUE, convert.data.frames = FALSE)
```

Arguments

`lst` list to be sorted.

`recursive` logical flag indicating whether to apply sorting recursively to all sublists. Defaults to TRUE. If FALSE, only the top-level entries in the list will be sorted.

`convert.data.frames` logical flag. If TRUE, data frames are converted to lists.

Value

Structured list with alphabetically sorted entries. If `recursive = TRUE`, all sublists are also sorted alphabetically. If the list contains unnamed elements, they are left unsorted.

Examples

```
# Create a nested list
my_list = list(
  b = list(d = 4, a = 2),
  empty = list(),
  'unnamed',
  a = 1,
  f = list(b = 3, a = list(d = seq(5), 'unnamed', c = 2))
)

# Sort the list recursively
sorted_list_recursive = sortlist(my_list)
print(sorted_list_recursive)
```

spectrumcolors	<i>Spectrum colour palette</i>
----------------	--------------------------------

Description

Generates smooth rainbow color scale from red to purple, similar to [rainbow](#), but with improved smoothness

Usage

```
spectrumcolors(n, alpha = 1, rev = FALSE)
```

Arguments

`n` integer number of colors in the scale

`alpha` alpha transparency value (0=fully transparent, 1=fully opaque)

`rev` logical flag indicating whether the ordering of the colors should be reversed

Value

Returns an n-vector of RGB colour strings.

Author(s)

Danail Obreschkow

```
#' @examples nplot() rasterImage(rbind(spectrumcolors(1e3)),0,0,1,0.5) rasterImage(rbind(rainbow(1e3,end=5/6)),0,0.5,1,1)
text(0.5,0.25,'spectrum') text(0.5,0.75,'rainbow') abline(h=0.5)
```

sph2car	<i>Spherical to Cartesian coordinate conversion</i>
---------	---

Description

Convert 3D spherical to Cartesian coordinates

Usage

```
sph2car(x)
```

Arguments

x	3-element or n-by-3 matrix representing the spherical components (r,theta,phi) of n three-dimensional vectors. Here, theta=0...pi is the polar angle measured from the north pole and phi=0...2*pi is the azimuth measured positively from the x-axis (ISO 80000-2:2019 physics convention).
---	--

Value

Returns a 3-element vector or a n-by-3 element matrix representing the Cartesian coordinates (x,y,z)

Author(s)

Danail Obreschkow

See Also

[car2sph](#)

sphereplot

Plot a spherical function or point set

Description

Plots a spherical function or a point set in a 2D projection using only standard R graphics. This avoids compatibility issues of rgl, e.g. knitting markdown documents.

Usage

```
sphereplot(
  f = NULL,
  n = 100,
  theta0 = pi/2,
  phi0 = 0,
  angle = 0,
  projection = "globe",
  col = gray.colors(256, 0, 1),
  clim = NULL,
  add = FALSE,
  center = c(0, 0),
  radius = 1,
  nv = 500,
  show.border = TRUE,
  show.grid = TRUE,
  grid.phi = seq(0, 330, 30)/180 * pi,
  grid.theta = seq(30, 150, 30)/180 * pi,
  pch = 16,
  pt.col = "black",
  pt.cex = 0.5,
  lwd = 0.5,
  lty = 1,
  line.col = "black",
  background = "white",
  ...
)
```

Arguments

f	must be either of: (1) NULL to plot just grid without spherical function (2) a vectorized real function f(theta,phi) of the polar angle theta [0,pi] and azimuth angle [0,2pi] (3) an n-by-2 array of values theta and phi
n	number of grid cells in each dimension used in the plot
theta0	polar angle in radians at the center of the projection

<code>phi0</code>	azimuth angle in radians at the center of the projection
<code>angle</code>	angle in radians between vertical axis and central longitudinal great circle
<code>projection</code>	type of projection: "globe" (default), "cylindrical", "mollweide"
<code>col</code>	color map
<code>clim</code>	2-element vector specifying the values of <code>f</code> corresponding to the first and last color in <code>col</code>
<code>add</code>	logical flag specifying whether the sphere is to be added to an existing plot
<code>center</code>	center of the sphere on the plot
<code>radius</code>	radius of the sphere on the plot
<code>nv</code>	number or vertices used for grid lines and border
<code>show.border</code>	logical flag specifying whether to show a circular border around the sphere
<code>show.grid</code>	logical flag specifying whether to show grid lines
<code>grid.phi</code>	vector of <code>phi</code> -values of the longitudinal grid lines
<code>grid.theta</code>	vector of <code>theta</code> -values of the latitudinal grid lines
<code>pch</code>	point type
<code>pt.col</code>	point color
<code>pt.cex</code>	point size
<code>lwd</code>	line width of grid lines and border
<code>lty</code>	line type of grid lines and border
<code>line.col</code>	color of grid lines and border
<code>background</code>	background color
<code>...</code>	additional arguments to be passed to the function <code>f</code>

Value

Returns a list containing the vector `col` of colors and 2-vector `clim` of values corresponding to the first and last color.

Author(s)

Danail Obreschkow

Examples

```
## Plot random points on the unit sphere in Mollweide projection
set.seed(1)
f = cbind(acos(runif(5000,-1,1)),runif(5000,0,2*pi))
sphereplot(f,theta0=pi/3,projection='mollweide',pt.col='red')

## Plot real spherical harmonics up to third degree
oldpar = par(mar=c(0,0,0,0))
nplot(xlim=c(-4,3.5),ylim=c(0,4),asp=1)
for (l in seq(0,3)) { # degree of spherical harmonic
  for (m in seq(-1,1)) { # order of spherical harmonic
```

```

# make spherical harmonic function in real-valued convention
f = function(theta,phi) sphericalharmonics(l,m,cbind(theta,phi))

# plot spherical harmonic
sphereplot(f, 50, col=planckcolors(100), phi0=0.1, theta0=pi/3, add=TRUE, clim=c(-0.7,0.7),
           center=c(m,3.5-1), radius=0.47)

if (l==3) text(m,-0.15,sprintf('m=%d',m))
}
text(-1-0.55,3.5-1,sprintf('l=%d',l),pos=2)
}
par(oldpar)

```

sphericalharmonics	<i>Spherical Harmonics</i>
--------------------	----------------------------

Description

Evaluates spherical harmonics Y , either in the real-valued or complex-valued basis.

Usage

```
sphericalharmonics(l, m, x, basis = "real")
```

Arguments

<code>l</code>	degree of the spherical harmonic, accurate to about $l=500$; (0=monopole, 1=dipole, 2=quadrupole, 3=octupole, 4=hexadecapole,...)
<code>m</code>	order of the spherical harmonic $(-l,-l+1,...,+l)$
<code>x</code>	either an n -by-2 matrix specifying the polar angle θ ($0 \dots \pi$) and azimuthal angle ϕ ($0 \dots 2\pi$); or an n -by-3 matrix specifying the 3D coordinates of n vectors (whose normalization is irrelevant).
<code>basis</code>	a string specifying the type of spherical harmonics; this has to be either "complex" for the standard complex-valued harmonics with Condon-Shortley phase convention, or "real" (default) for the standard real-valued harmonics.

Value

Returns an n -vector of the spherical harmonics; for points $x=c(0,0,0)$, a value of 0 is returned

Author(s)

Danail Obreschkow

Examples

```
## Check orthonormalization of all spherical harmonics up to 3rd degree

# make indices l and m up to 3rd degree
l = c(0,rep(1,3),rep(2,5),rep(3,7))
m = c(0,seq(-1,1),seq(-2,2),seq(-3,3))

# check orthonormalization for all pairs
for (i in seq(16)) {
  for (j in seq(16)) {

    # compute scalar product
    f = function(theta,phi) {
      Yi = sphericalharmonics(l[i],m[i],cbind(theta,phi))
      Yj = sphericalharmonics(l[j],m[j],cbind(theta,phi))
      return(Re(Yi*Conj(Yj))*sin(theta))
    }
    g = Vectorize(function(phi) integrate(f,0,pi,phi)$value)
    scalar.product = integrate(g,0,2*pi)$value

    # compare scalar product to expected value
    ok = abs(scalar.product-(i==j))<1e-6
    cat(sprintf('(l=%1d,m=%+1d|l=%1d,m=%+1d)=%5.3f  %s\n',l[i],m[i],l[j],m[j],
      scalar.product+1e-10,ifelse(ok,'ok','wrong'))))
  }
}
```

streamlines

Draw streamlines of a two-dimensional vector field

Description

Draws streamlines of a planar vector field $f(x, y)$ by integrating forward and backward from a set of starting points. Starting points can be provided as a single integer, a length-2 integer vector, or an $n \times 2$ matrix of coordinates.

Usage

```
streamlines(
  f,
  xlim,
  ylim,
  points = 20,
  nsteps = 100,
  arrows = FALSE,
  add = FALSE,
  ...
)
```

Arguments

<code>f</code>	A function of the form ‘ <code>f(x, y)</code> ’ returning an $n \times 2$ matrix of vector components, where the first column is the x-component and the second column is the y-component.
<code>xlim</code>	Numeric vector of length 2 giving the x-limits of the plot.
<code>ylim</code>	Numeric vector of length 2 giving the y-limits of the plot.
<code>points</code>	Starting points for the streamlines. This can be: • a single integer, interpreted as the number of quasi-random starting points; • a numeric vector of length 2, interpreted as the numbers of starting points in x- and y-direction; • a numeric matrix with 2 columns, giving explicit starting coordinates.
<code>nsteps</code>	Integer giving the number of integration steps in each direction.
<code>arrows</code>	Controls where arrows are drawn. This can be: • ‘FALSE’: no arrows are drawn; • ‘TRUE’: one arrow is drawn on every streamline, centered on its starting point and aligned with the local field direction; • an integer vector: arrows are drawn only on the corresponding streamlines, using the indices of the starting points; • a numeric matrix with 2 columns: arrows are drawn at the specified coordinates, aligned with the local field direction at those points.
<code>add</code>	Logical; if ‘FALSE’ a new plot is created, otherwise streamlines are added to the existing plot.
<code>...</code>	Further graphical parameters passed to <code>[graphics::lines()]</code> and <code>[graphics::arrows()]</code> .

Details

The integration uses a fixed step length based on the plot diagonal,

$$d = \sqrt{dx^2 + dy^2} / nsteps,$$

where ‘`dx = diff(range(xlim))`’ and ‘`dy = diff(range(ylim))`’. At each step, only the direction of the vector field is used, via `[unitvector()]`, so the result shows streamlines of the field rather than trajectories with speed information.

If ‘`add = FALSE`’, a new plot is initialized using `[plot()]`.

Arrows are drawn along the local field direction. If ‘`arrows = TRUE`’, each arrow is centered on the streamline starting point. If ‘`arrows`’ is a matrix of coordinates, the arrows are placed at those coordinates, regardless of whether they lie exactly on a streamline.

Value

Invisibly returns a list with components:

- ‘forward’: array of forward-integrated coordinates;
- ‘backward’: array of backward-integrated coordinates;
- ‘start’: matrix of starting coordinates.

Examples

```
f = function(x,y) {
  vx = -x-y
  vy = -y+(x-0.5)
  cbind(vx,vy)
}

streamlines(f, c(-1,1), c(-1,1), 50, 500, col = "#5555ff")
streamlines(f, c(-1,1), c(-1,1), 20, 200, arrows = TRUE, add = FALSE,
  col = "#5555ff")
```

stretch	<i>Stretch values to a custom range</i>
---------	---

Description

Shifts and stretches the values of a vector or array to a desired interval, while maintaining the shape of the input argument

Usage

```
stretch(x, min = 0, max = 1, invert = FALSE, gamma = NULL, na = NULL)
```

Arguments

x	vector or array
min	minimum value
max	maximum value
invert	logical flag specifying whether the data should be inverted, such that the smallest input value maps to max and the largest input value maps to min.
gamma	optional argument specifying a non-linear transformation $x \rightarrow x^\gamma$, if $\gamma > 0$, or $x \rightarrow 1 - (1-x)^{-\gamma}$, if $\gamma < 0$.
na	optional value specifying the value assigned to non-numbers (NA and NaN)

Value

vector/array of the same shape as x

Author(s)

Danail Obreschkow

See Also

lim

 subplot

Insert a sub-panel into plot

Description

Insert a sub-panel into an existing plotting area. To open a subplot, call `par(subplot(...))`, to close it, you must call `par(subplot('off'))`.

Usage

```
subplot(xleft = NA, ybottom, xright, ytop)
```

Arguments

<code>xleft</code>	lower x-coordinate of the sub-panel relative to the current plot.
<code>ybottom</code>	lower y-coordinate of the sub-panel relative to the current plot.
<code>xright</code>	upper x-coordinate of the sub-panel relative to the current plot.
<code>ytop</code>	upper y-coordinate of the sub-panel relative to the current plot.

Value

graphical parameters to user with [par](#).

Author(s)

Danail Obreschkow

Examples

```
# main plot
f = function(x) x*sin(1/(x+.Machine$double.eps))
curve(f,0,1,n=1000,ylim=c(-1,1),xlab='',ylab='',xaxs='i',yaxs='i')
rect(0.02,-0.1,0.1,0.1,border='blue',col=transparent('blue',0.2))

# subplot
par(subplot(0.55,-0.8,0.93,0))
curve(f,0.02,0.1,n=500,ylim=c(-0.1,0.1),xlab='',ylab='',xaxs='i',yaxs='i')
rect(0.02,-0.1,0.1,0.1,border=NA,col= transparent('blue',0.2))
par(subplot('off'))
```

tick	<i>Start timer</i>
------	--------------------

Description

Start timer and write a custom text into the console.

Usage

```
tick(txt = "Start")
```

Arguments

txt custom text to be displayed.

Value

None

Author(s)

Danail Obreschkow

See Also

[tock progress error](#)

Examples

```
tick('Sum 10 million random numbers')
x = sum(runif(1e7))
tock()
```

tock	<i>Stop timer</i>
------	-------------------

Description

Stop timer and write the computation in seconds since the last call of tick().

Usage

```
tock(txt = "", fmt = " (%.2fs). %s\n")
```

Arguments

txt	custom text to be displayed.
fmt	character vector of format strings. It must contain exactly one %s as placeholder for txt and one numerical format, such as %f or %e, as placeholder for the time.

Value

Returns the elapsed time in seconds since calling tick().

Author(s)

Danail Obreschkow

See Also

[tick progress error](#)

Examples

```
tick('Sum 10 million random numbers')
x = sum(runif(1e7))
tock()
```

transparent

Add transparency to a color

Description

Add transparency to a color

Usage

```
transparent(col, alpha = 0.5)
```

Arguments

col	is a color or vector/array of colors, specified as text (e.g. 'purple') or 7/9-character (e.g. '#A020F0')
alpha	transparency value between 0 and 1 or a vector/array thereof

Value

Returns a 9-character color or vector/array of 9-character colors.

Author(s)

Danail Obreschkow

See Also[lightness](#)**Examples**

```
# Add different transparencies of the same color
plot(runif(50),runif(50),pch=20,cex=10,col=transparent('purple',runif(50)))

# Add the same transparency to different colors
plot(runif(50),runif(50),pch=20,cex=10,col=transparent(rainbow(50)))
```

transzoom

*Zoom, translate and rotate array image***Description**

Zoom/rotate/translate an image relative to its center for images represented as simple arrays.

Usage

```
transzoom(
  img = NULL,
  zoom = 1,
  shift = c(0, 0),
  angle = 0,
  size = NULL,
  col = "black",
  filter = "bilinear",
  file.in = "",
  file.out = "",
  format = "png",
  show.image = TRUE
)
```

Arguments

<code>img</code>	n-by-m-by-3 array or n-by-m-by-4 array representing an rgb(+alpha) image.
<code>zoom</code>	zoom factor (>0).
<code>shift</code>	2-vector specifying the vertical+horizontal translation in units of output pixels (i.e. after zooming).
<code>angle</code>	rotation angle in degrees.
<code>size</code>	2-vector specifying the vertical+horizontal dimensions of the output image. If not given, this is taken to be identical to the input image.
<code>col</code>	background color

filter	affine transformation filter; either 'none' or 'bilinear'
file.in	optional input filename, which can be used to load an image instead of providing it via img. This filename is ignored if img is specified.
file.out	optional output filename.
format	one of "png" or "jpg" specifying the file format of the input and output image.
show.image	logical flag specifying whether the image is displayed in the R console.

Value

Returns an n-by-m-by-3 array or n-by-m-by-4 array of the processed image.

Author(s)

Danail Obreschkow

Examples

```
img = yinyangyong # this is an example image included in the package
transzoom(img, zoom=2) # zoom by a factor 2
```

uniquedouble	<i>Map positive 64-bit integers onto unique doubles</i>
--------------	---

Description

Uses a reversible one-to-one mapping to converts non-negative 64-bit integers, produced via the bit64 package, to double-precision floating-point values for faster handling of 64-bit integer indices, e.g. comparison of indices, count number of unique indices, etc. The double values are completely different from the corresponding integer values.

Usage

```
uniquedouble(x, inverse = FALSE)
```

Arguments

x	If inverse=FALSE (default), this is a scalar/vector/array of non-negative integers, typically 64-bit integers. If inverse=TRUE, it is a scalar/vector/array of doubles.
inverse	Logical flag. If TRUE, doubles are converted back to their original 64-bit integers.

Value

Scalar/vector/array of double values, if inverse=FALSE, or integer64 values, if inverse=TRUE.

Author(s)

Danail Obreschkow

Examples

```
# produce example vector of non-negative 64-bit integers
n = 1e3
x = c(bit64::as.integer64(0:n),
      bit64::as.integer64('9218868437227405311')+c(-n:n),
      bit64::lim.integer64()[2]-c(0:n))

# map this vector onto unique doubles
y = uniquedouble(x)

# check if the double-vector can be inverted back to the integer-vector
cat(sprintf("Check inversion = %s.\n", all(x==uniquedouble(y, inverse=TRUE))))

# measure the time taken to compare all the int64 values
tick("Compare original integer64 values. ")
comparison = TRUE
for(i in seq_along(x)) comparison = comparison & x[i]==x[i]
tock(comparison, fmt="Time taken = %.3fs. Test result = %s.\n")

# measure the time taken to compare all the corresponding double values
tick("Compare corresponding double values. ")
comparison = TRUE
for(i in seq_along(y)) comparison = comparison & y[i]==y[i]
tock(comparison, fmt="Time taken = %.3fs. Test result = %s.\n")
```

unitvector

*Normalize vectors to unit length***Description**

Computes unit vectors from one or more vectors.

Usage

```
unitvector(x)
```

Arguments

x Numeric vector or matrix. If a matrix is supplied, each row is interpreted as a vector.

Value

An object of the same type and dimensions as **x**, with each vector normalized to unit length. Zero vectors are returned unchanged.

See Also

[vectornorm](#)

userattributes

Retrieve Custom Object Attributes

Description

This function takes a generic R object and returns the custom attributes added by the user, distinguishing them from the object's inherent attributes.

Usage

```
userattributes(obj)
```

Arguments

obj R object whose custom attributes to extract.

Value

Named list of custom attributes, mimicking the output of the base function [attributes](#), but only including custom attributes

See Also

[attributes](#)

Examples

```
# Create a list containing objects of different classes
example = list(1,
               as.integer(1:3),
               bit64::as.integer64(1),
               diag(5),
               array(0,c(2,3,5)),
               list(a=1,b='c'),
               data.frame(x=1, y=1:10, char=LETTERS[1:10])
)

# Loop over all the objects to check if the custom attribute is correctly extracted.
for (i in seq_along(example)) {
  x = example[[i]]
  attr(x, 'MyAttribute') = 'Test'
  cat(sprintf('Class = %s, Custom attribute(s) = %s\n', class(x)[1],
              paste(names(userattributes(x)), collapse = ', ')))
}
```

vectornorm	<i>Vector norm</i>
------------	--------------------

Description

Compute the norm of a vector or a matrix of vectors

Usage

```
vectornorm(x)
```

Arguments

x	m-element vector or n-by-m matrix (x[1:n,l:m]) representing n m-element vectors
---	---

Value

Returns a scalar or an n-element vector with the vector norms

Author(s)

Danail Obreschkow

See Also

[vectornorm](#)

vectorproduct	<i>Vector product</i>
---------------	-----------------------

Description

Computes the vector (cross) product of two three-dimensional vectors. The inputs may be individual vectors or matrices whose rows represent vectors.

Usage

```
vectorproduct(x, y, normalize = FALSE)
```

Arguments

x, y	Numeric vectors of length three or matrices with three columns. If a matrix is supplied, each row is interpreted as a vector.
normalize	Logical flag indicating whether the resulting vector(s) should be normalized to unit length.

Value

Returns either a 3-element vector or an $n \times 3$ matrix containing the row-wise vector products.

See Also

[scalarproduct](#), [vectornorm](#), [unitvector](#)

wavelength2col	<i>Convert wavelength to RGB</i>
----------------	----------------------------------

Description

Converts a given wavelength of light to an approximate RGB color value, using black in the invisible range.

Usage

```
wavelength2col(wavelength)
```

Arguments

wavelength wavelength value (or vector), in nanometers.

Value

Returns a color string or vector of color strings with the same number of elements as wavelength.

Author(s)

Danail Obreschkow

Source

Smoothed implementation of the original Fortran version by Dan Bruton (<http://www.physics.sfasu.edu/astro/color/spectra.htm>) and the R-function by Michael Friendly (<https://gist.github.com/friendly>).

Examples

```
lambda = seq(300,800)
col = matrix(wavelength2col(lambda),nrow=1)
plot(NA,xlim=range(lambda),ylim=c(0,1),xaxs='i',xlab='wavelength [nm]',yaxs='i',yaxt='n',ylab='')
rasterImage(col,min(lambda),0,max(lambda),1)
```

writehdf5

*Write structured list to an HDF5 file***Description**

Writes a named list, including its hierarchy of nested sublists, to an HDF5 file with HDF5 groups, subgroups and datasets preserving the hierarchical structure. The routine supports standard HDF5 data types, including double-precision floating point numbers (64 bit), integers (32 bit), characters (8 bit), and booleans, as well as vectors and arrays of these types. It also supports 64-bit integers (H5T_NATIVE_INT64), available via the `bit64` package, as well as 32-bit floating-point objects of class `float32`. Custom attributes of sublists and data, assigned in R via `attr`, are automatically transcribed to group and dataset attributes in the HDF5 file. Such attributes can also be provided for empty groups (produced by `list()`) and datasets (produced by `numeric()`).

Usage

```
writehdf5(obj, file, inherent.attributes = FALSE, level = 6, overwrite = TRUE)
```

Arguments

<code>obj</code>	List containing the data to be written. Nested sublists are interpreted as subgroups within the HDF5 file. If a sublist is empty or if an element inside a list is 'NULL', it creates an empty group/dataset that can hold only attributes.
<code>file</code>	Character string specifying the file name of the output HDF5 file.
<code>inherent.attributes</code>	Logical flag indicating whether to include inherent attributes that some R-objects possess, such as 'dim' for matrices or 'names' for named vectors and arrays.
<code>level</code>	Integer specifying the compression level for datasets, typically between 0 (no compression) and 9 (maximum compression). Not all dataset types support compression.
<code>overwrite</code>	Logical value indicating whether to overwrite an existing file.

Details

The function relies on the `hdf5r` package and on the `bit64` package.

The nested list `obj` should only contain data types available to HDF5. The only exception are data frames, which, if included, are automatically converted to lists. Normally, the list `obj` and its nested sublists, should all be named lists, i.e. `list(a=1, b=2)` rather than `list(1,2)`. Unnamed elements are automatically assigned a name 'unnamed_#' in the HDF5 file.

Some data types in R have inherent attributes, such as 'names' for data frames and 'dim' for arrays. By default, these inherent attributes are not written to the HDF5 file. They are, however, automatically regenerated when the HDF5 file is loaded back via `readhdf5`. The argument `inherent.attributes` can be used to force writing all attributes, including the inherent ones, to the HDF5 file.

If a structured R list is saved with `writehdf5` and then reloaded using `readhdf5`, the recovered list is identical to the input list up to the ordering of list elements, which is alphabetic by default in HDF5. The only other difference between the input and recovered data occurs when the input data contain data frames, as these are automatically converted to lists. A workaround is to set `inherent.attributes=TRUE` when writing the HDF5 file. In this case, the reloaded HDF5 data becomes a data frame again.

Value

None

See Also

[readhdf5](#)

Examples

```
# Create example data
input = list(
  group_empty = list(),
  dataset_empty = numeric(0),
  group_dataframe = data.frame(
    ID = as.integer(1:3),
    Name = c("Alice", "Bob", "Charlie"),
    Salary = c(2341.2, 3534.2, 4541.9),
    Employed = c(TRUE, TRUE, FALSE)
  ),
  dataset_parameters = 1.234,
  group_integers = list(int32 = as.integer(123),
    int64 = bit64::as.integer64(123),
    vector = bit64::as.integer64((1:3)+12345678912345)),
  dataset_nonnumeric = c(NA, NaN, Inf, -Inf),
  group_mixed = list(
    header = 'test header',
    subgroup1 = list(
      dataset1 = c("A", "%}~&^", "x1y2z3", "", " "),
      dataset2 = matrix(as.integer(1:10), nrow = 2),
      dataset3 = array(runif(30), dim = c(2, 5, 3))
    ),
    subgroup2 = list(date = as.character(as.Date("2025-01-01")),
      location = 'Perth')
  )
)

# Add attributes to some datasets
attr(input$dataset_empty, 'Comment') = 'This is a test file.'
attr(input$group_mixed$subgroup1$dataset3, 'Type') = '3D array'
attr(input$group_integers$vector, 'Comment') = 'Vector of long integers'
attr(input$group_integers$vector, 'Package') = 'bit64'

# Add attributes to some groups
```

```
attr(input$group_dataframe,'Company branch') = 'Sales'
attr(input$group_integers,'Comment') = 'Testing different integers'
attr(input$group_empty,'Timestamp') = date()
attr(input$group_empty,'Working directory') = getwd()

if (requireNamespace("hdf5r", quietly = TRUE)) {

  # Write list to HDF5 file
  filename = tempfile()
  writehdf5(input, filename)

  # Read HDF5 file into a new list
  output = readhdf5(filename)

  # Check if input and output lists are identical
  # (up to alphabetic ordering and data frame-to-list conversion)
  print(all.equal(sortlist(input, convert.data.frames = TRUE), output))

  # Write list to HDF5 file again, this time with inherent attributes
  filename = tempfile()
  writehdf5(input, filename, inherent.attributes = TRUE)

  # Read HDF5 file into a new list
  output = readhdf5(filename)

  # Check if input and output lists are identical
  # (up to alphabetic ordering only)
  print(all.equal(sortlist(input), output))
}
```

yinyangyong

Yin-Yang-Yong image

Description

A data set containing a 500-by-500-by-4 array, representing an image of a Yin-Yang-Yong symbol with transparency. This symbol was 'reinvented' many times. The particular version in this package is the one drawn by the package author Danail Obreschkow in 1999.

Usage

```
yinyangyong
```

Format

An object of class array of dimension 500 x 500 x 4.

Value

None

Author(s)

Danail Obreschkow

Examples

```
nplot(asp=1)  
rasterImage(yinyangyong,0,0,1,1)
```

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